

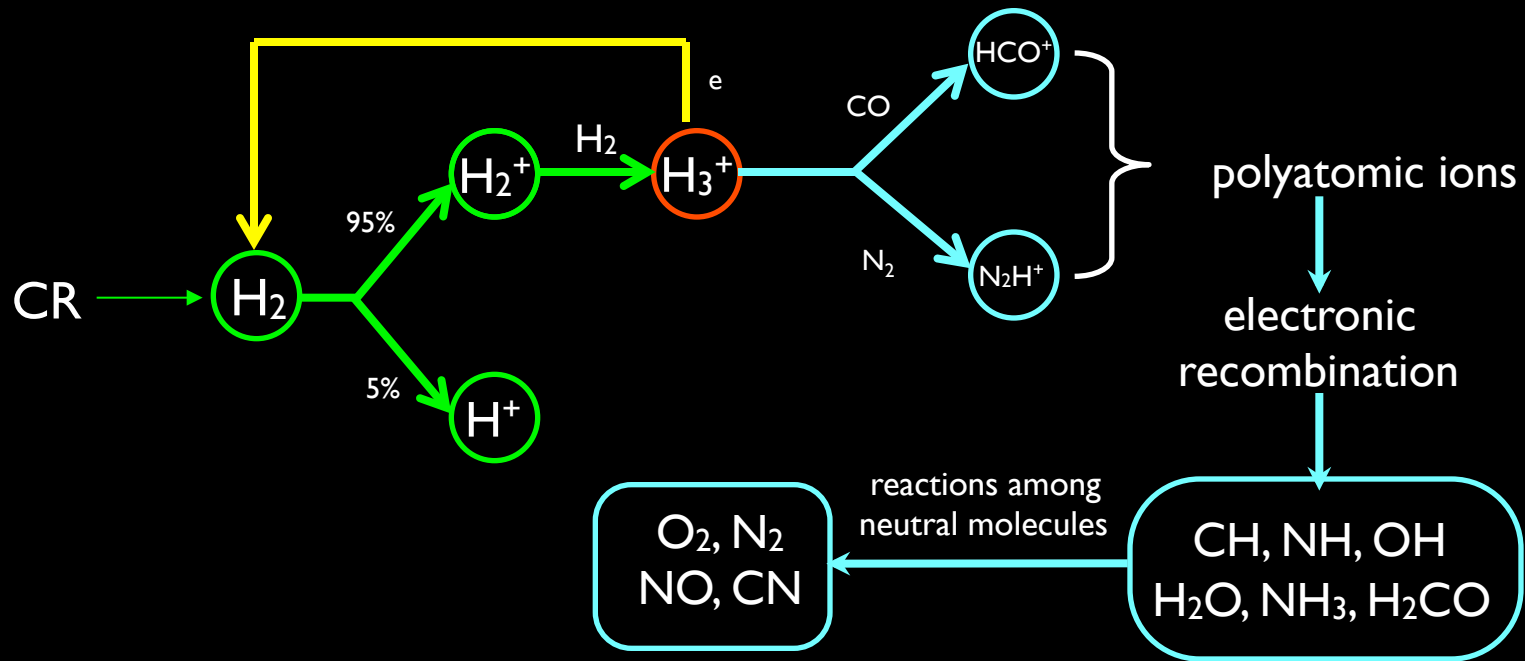
Gas-phase chemistry in the ISM and the primordial Universe

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Fundamental gas-phase reactions in molecular clouds



Reactions and reaction rates

- $A+B \rightarrow P$ (two-body reaction)

$$\frac{dn_P}{dt} = k n_A n_B \quad \text{units of } k : \text{cm}^3 \text{ s}^{-1}$$

- $A+\text{photon} \rightarrow P$ (photoreaction)

$$\frac{dn_P}{dt} = k n_A \quad \text{units of } k : \text{s}^{-1}$$

- $A+B+C \rightarrow P$ (three-body reaction)

$$\frac{dn_P}{dt} = k n_A n_B n_C \quad \text{units of } k : \text{cm}^6 \text{ s}^{-1}$$

Two-body reactions, thermal rate

$$k(T) = \int_0^\infty \sigma(v) v f(v) 4\pi v^2 dv \equiv \langle \sigma v \rangle$$

Where σ is the cross section of the process and $f(v)$ the maxwellian distribution of relative velocities

$$f(v) = \left(\frac{\mu}{2\pi k_B T} \right)^{3/2} \exp \left(-\frac{\mu v^2}{2k_B T} \right)$$

Chemical networks

A system of ODEs

$$\frac{dx_P}{dt} = k_{2b}(T_{\text{gas}})n x_A x_B + k_{3b}(T_{\text{gas}}) n^2 x_A x_B x_C - k_d(T_{\text{rad}})x_P + \dots$$

for the fractional abundances

$$x_i \equiv \frac{n_i}{n}$$

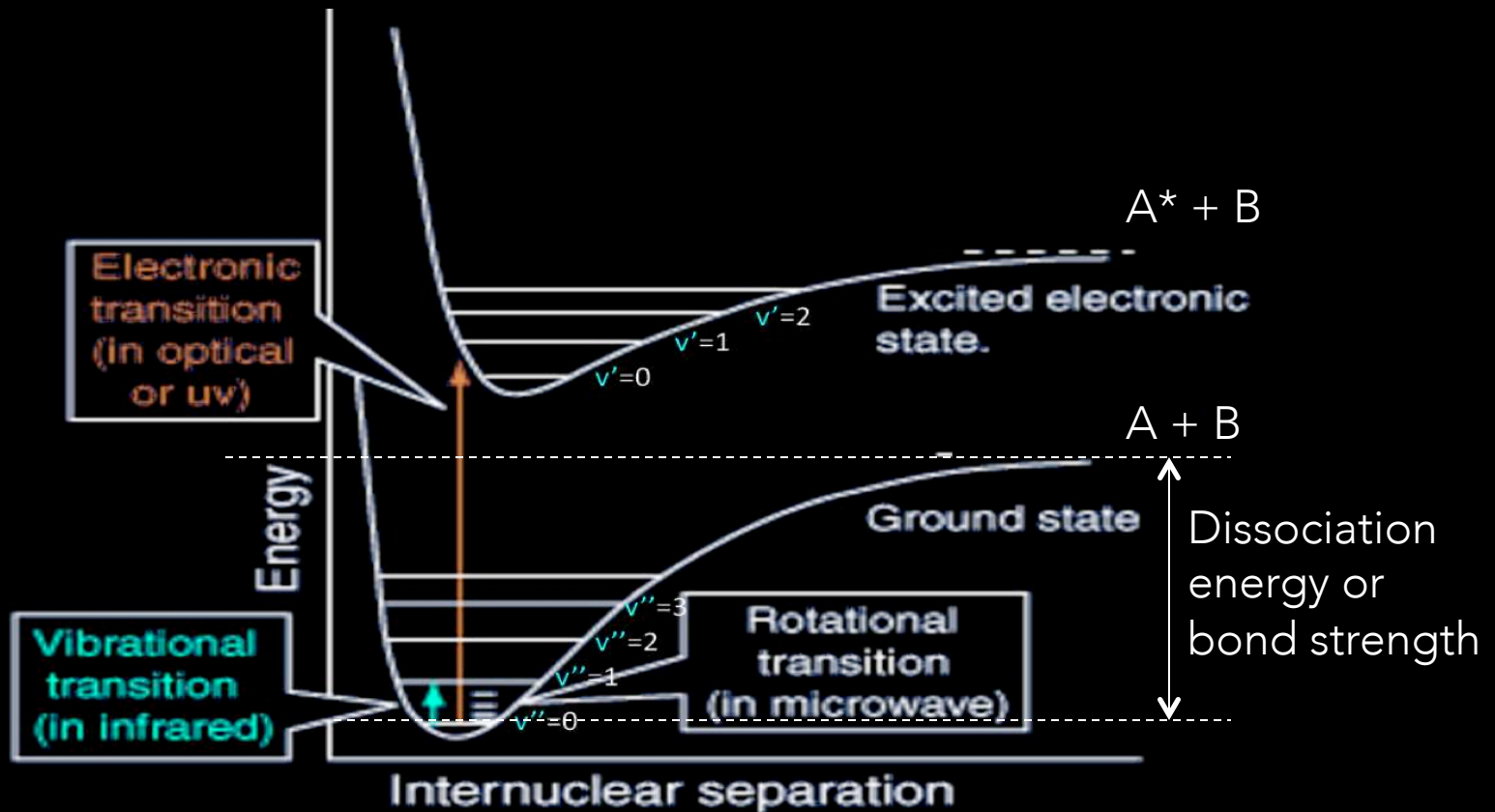
k_{2b} , k_{3b} depend on T_{gas} ; k_d depend on spectrum (photons, CRs)
Usually $k \sim T_{\text{gas}}^\alpha$, but activation energy $k \sim \exp(-E_A/k_B T_{\text{gas}})$

Needs n , T_{gas} , T_{rad}

- $n(r)$, $T_{\text{gas}}(r)$, $T_{\text{rad}}(r)$ fixed (e.g. cloud chemistry)
- $n(t)$, $T_{\text{gas}}(t)$, $T_{\text{rad}}(t)$ prescribed (e.g. early Universe)
- $n(r,t)$, $T_{\text{gas}}(r,t)$, $T_{\text{rad}}(r,t)$ dynamics-chemistry coupled (e.g. star formation)

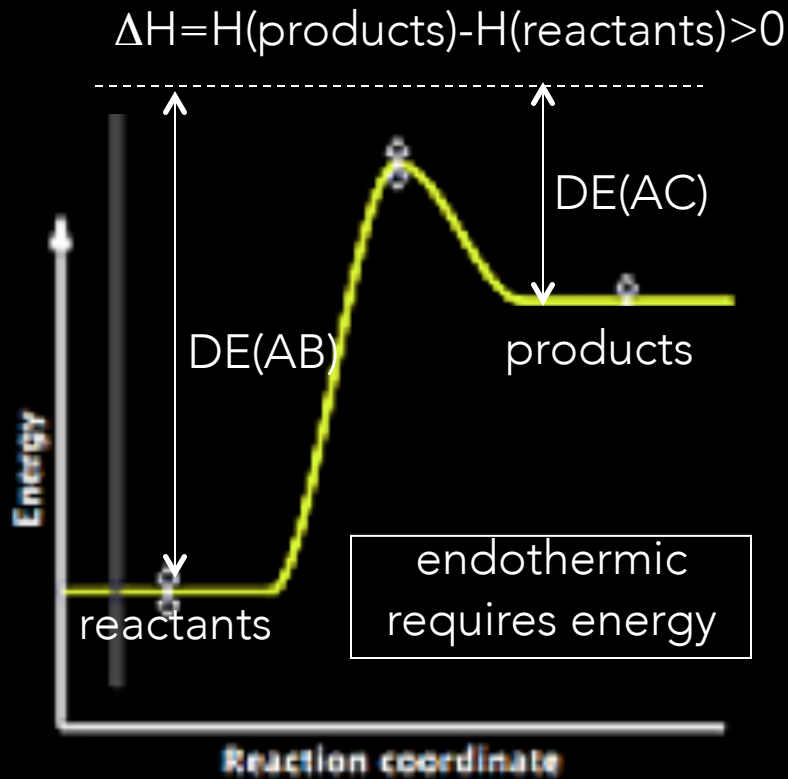
→ see talk by T. Haugbølle on Tuesday

Energy levels of a diatomic molecule

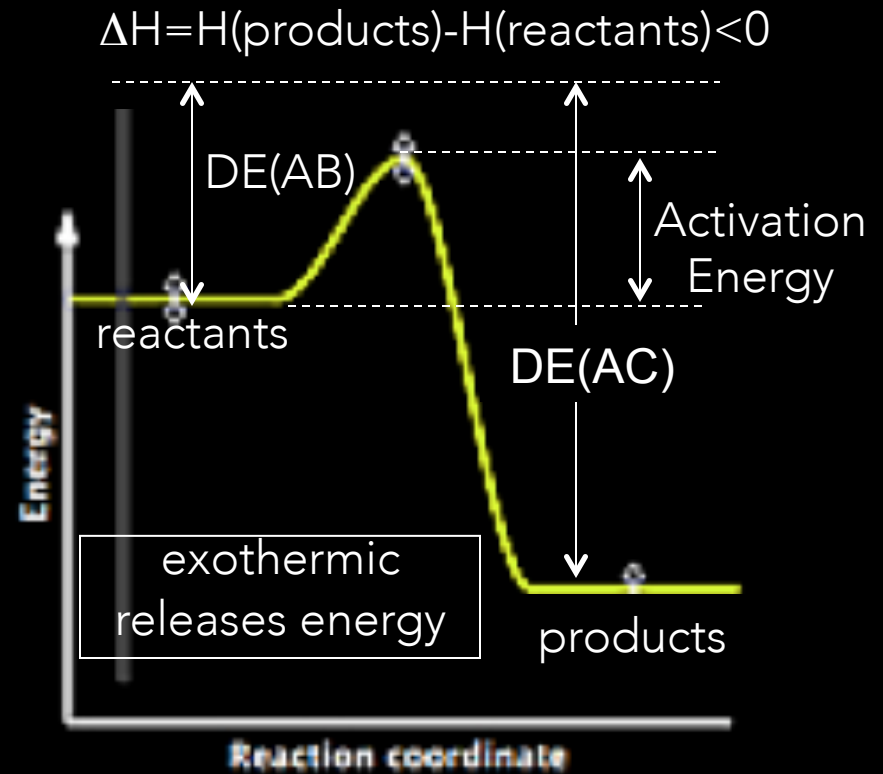


Chemical reactions in the ISM

- Low temperatures: $T=10\text{-}100\text{ K}$, $E=1\text{-}10\text{ meV}$.
Only exothermal reactions are possible
- Low density: $n=10^3\text{-}10^6\text{ cm}^{-3}$. Only two-body reactions.
(3-b frequent in the Earth's atmosphere $n=10^{19}\text{ cm}^{-3}$)
- Some reactions, even if exothermal, have a potential barrier (activation energy). Not possible if the temperature is too low.
- Shocks and turbulence generate warm zones where endothermal reactions can occur (shock chemistry)



$C^+ + H_2 \rightarrow CH^+ + H$
 $DE(H_2) = 4.5 \text{ eV}$
 $DE(CH^+) = 4.1 \text{ eV}$
 endothermic by 0.4 eV
 (important in shocks)



$OH + H_2 \rightarrow H_2O + H$
 $DE(H_2) = 4.5 \text{ eV}$
 $DE(H_2O) = 5.1 \text{ eV}$
 but 0.14 eV barrier
 (important in shocks and hot cores)

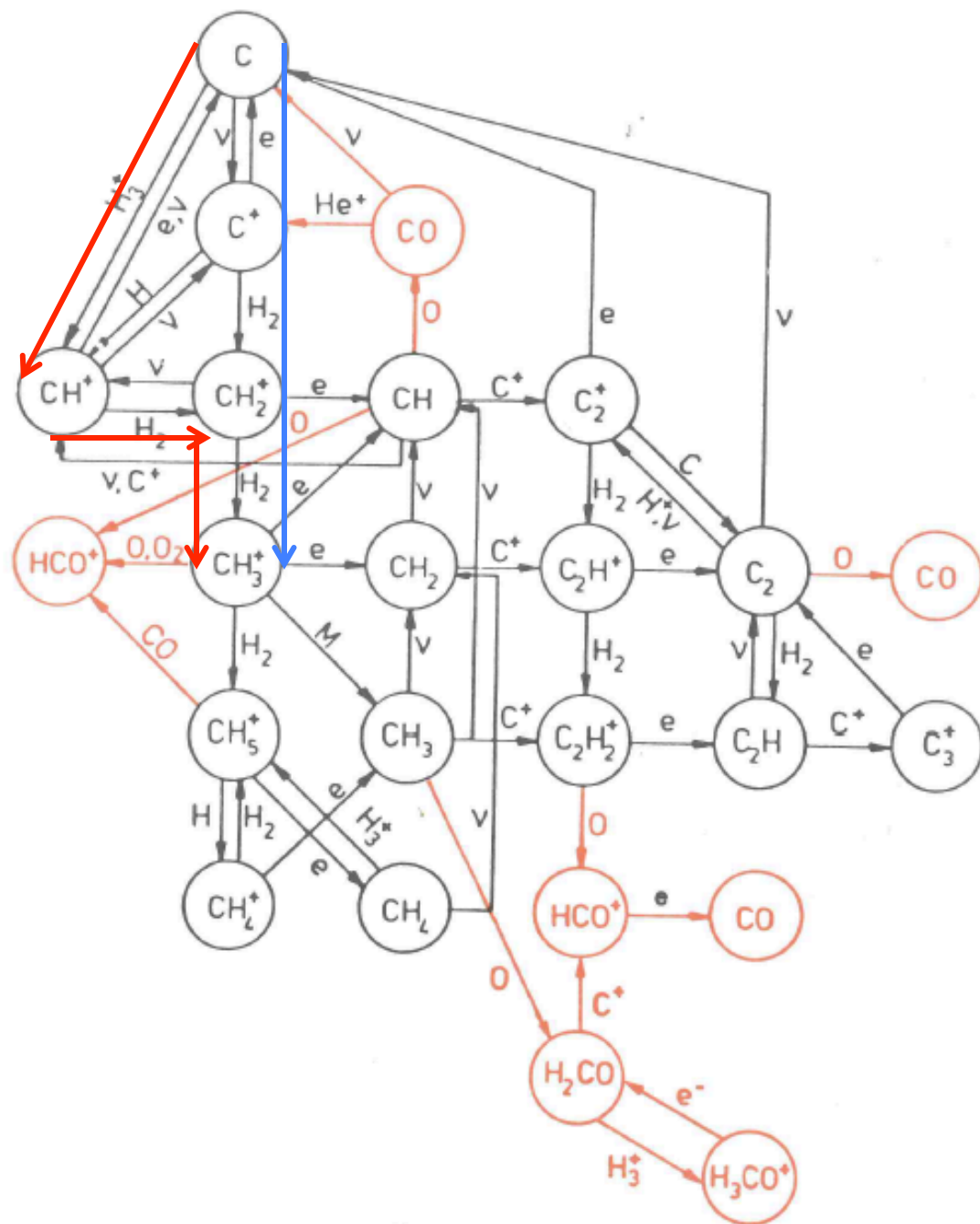
C chemistry

in diffuse clouds

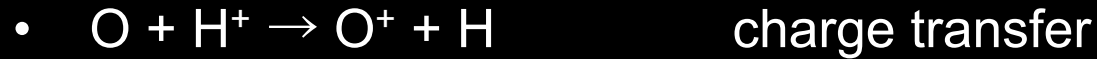
- $\text{C} + \text{ISRF (IP 13.3eV)} \rightarrow \text{C}^+ + \text{e}$ ($x_e = 10^{-4}$)
- $\text{C}^+ + \text{H}_2 \rightarrow \text{CH}^+$ NO (endothermic $\Delta E = 0.4 \text{ eV}$)
- $\text{C}^+ + \text{H}_2 \rightarrow \text{CH}_2^+$ radiative association, slow

in dense clouds

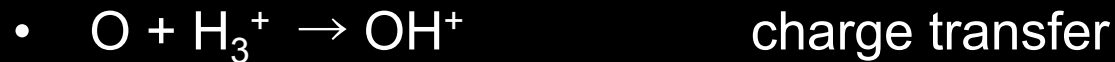
- $\text{C} + \text{H}_2 \rightarrow \text{CH}$ NO (endothermic $\Delta E = 1 \text{ eV}$)
- $\text{C} + \text{H}_3^+ \rightarrow \text{CH}^+$ charge transfer, fast
- $\text{CH}^+ + \text{H}_2 \rightarrow \text{CH}_2^+$
- $\text{CH}_2^+ + \text{H}_2 \rightarrow \text{CH}_3^+$ } hydrogen abstraction
- $\text{CH}_3^+ + \text{e} \rightarrow \text{CH}, \text{CH}_2$ dissociative recombination
- formation of hydrocarbons



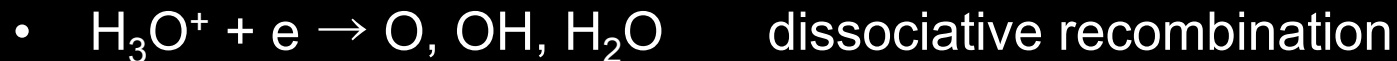
O chemistry

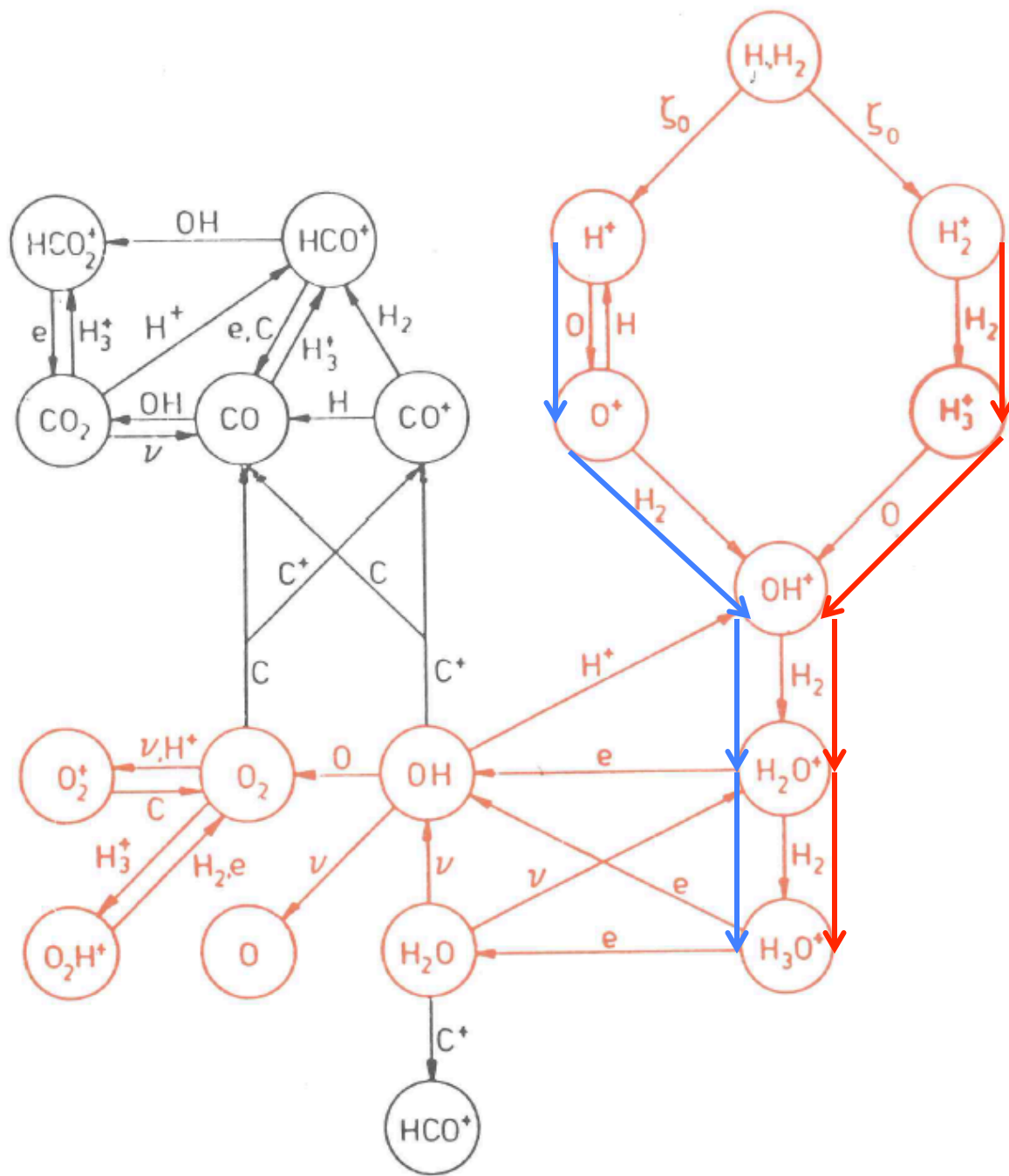


or



followed by





Types of reactions

Collisional processes:

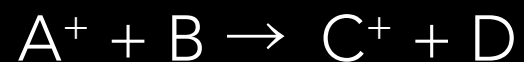
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|-------------------------------|-------------------------------|
| 1. ion-neutral reactions | $A^+ + B \rightarrow C^+ + D$ |
| 2. radiative association | $A + B \rightarrow AB + h\nu$ |
| 3. dissociative recombination | $AB^+ + e \rightarrow A + B$ |
| 4. neutral-neutral reactions | $A + B \rightarrow C + D$ |
| 5. charge transfer | $A^+ + B \rightarrow A + B^+$ |

Photoprocesses:

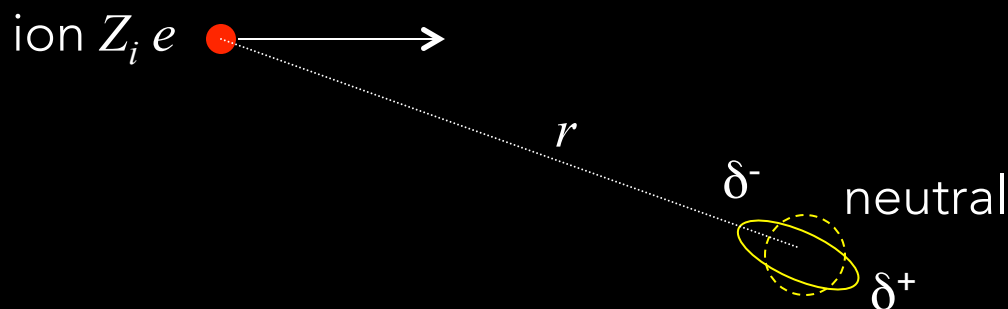
- | | |
|----------------------|----------------------------------|
| 1. photodissociation | $AB + h\nu \rightarrow A + B$ |
| 2. photoionization | $AB + h\nu \rightarrow AB^+ + e$ |

(see talks by W.-F. Thi, T. Grassi, D. Seifried on Wednesday)

1. Ion-neutral reactions

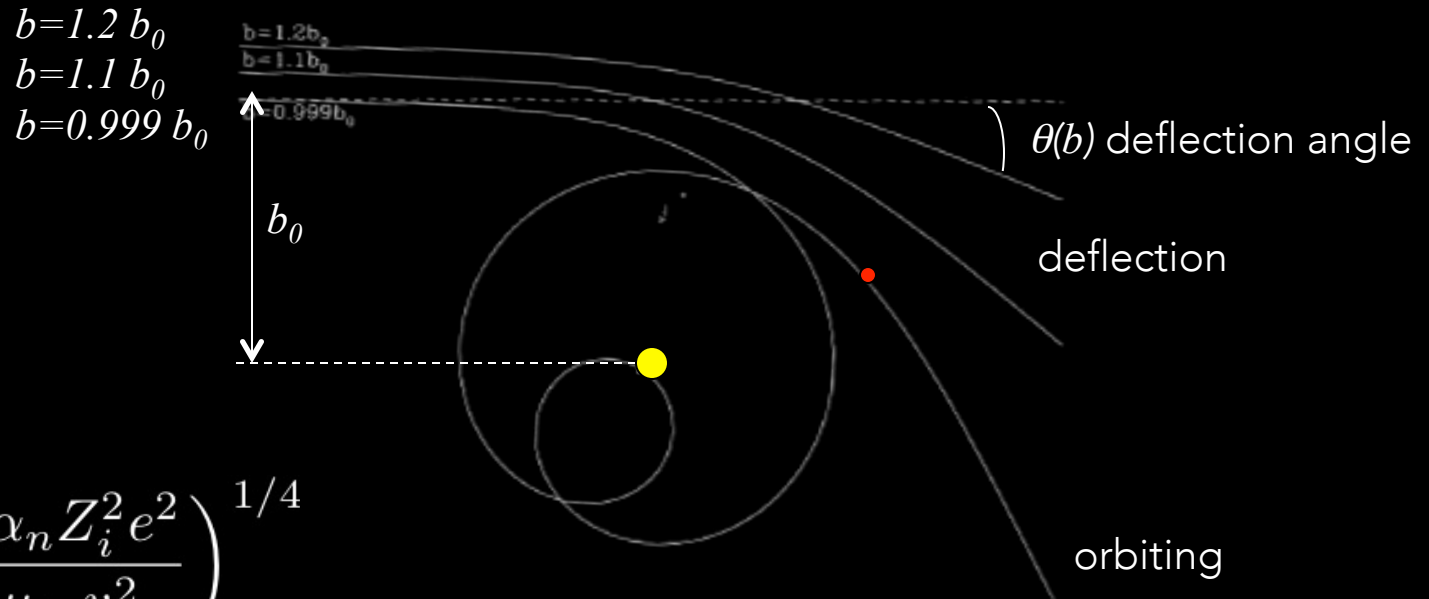


- Often have no activation barrier
- The approaching ion induces an electric dipole in the neutral that attracts the ion



- Long-range attractive potential $V_{in} = -\frac{\alpha_n Z_i^2 e^2}{2r^4}$
 $\alpha_n \approx 1 \text{ \AA}^3$ polarizability of neutral species

Orbits in r^{-4} potential

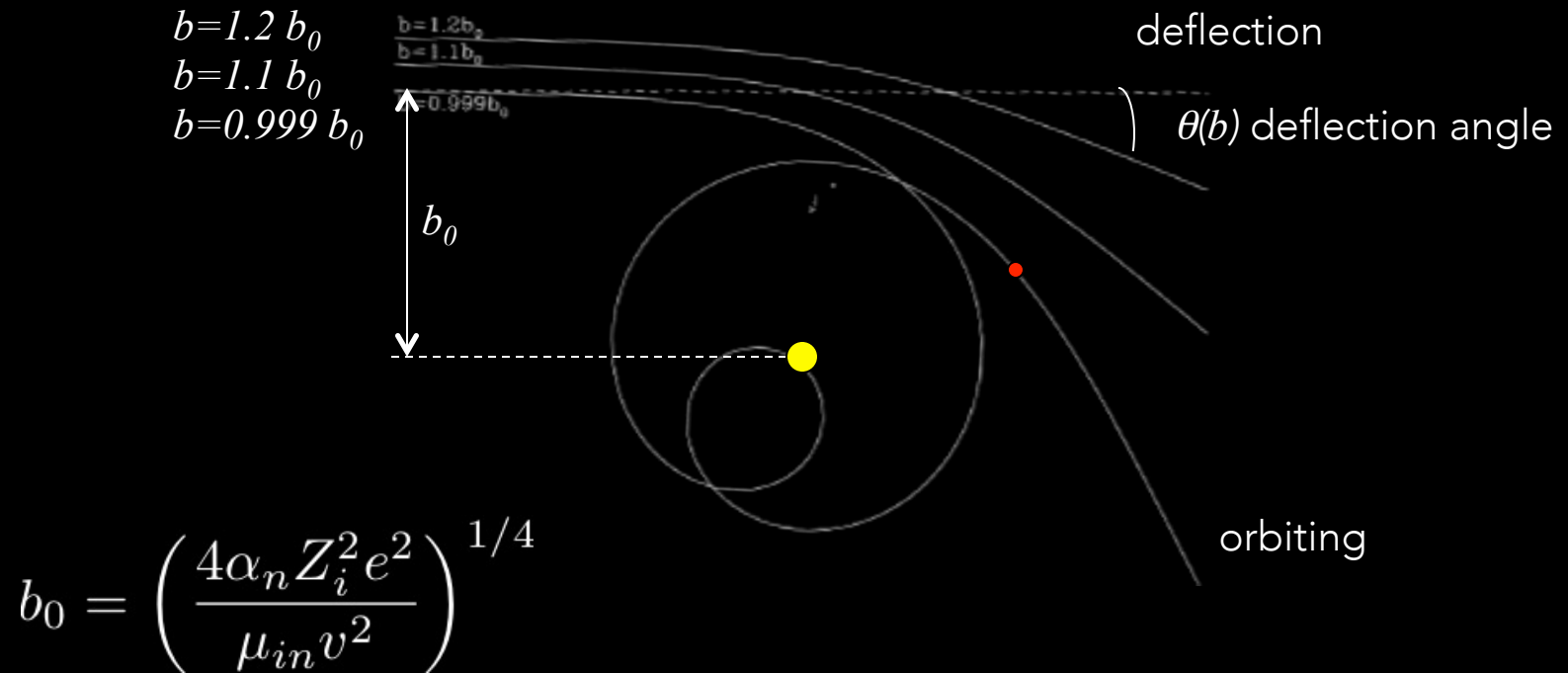


$$b_0 = \left(\frac{4\alpha_n Z_i^2 e^2}{\mu_{in} v^2} \right)^{1/4}$$

$$\sigma = \pi b_0^2 = 2\pi Z_i e \left(\frac{\alpha_n}{\mu_{in}} \right)^{1/2} \frac{1}{v} \quad \text{Langevin cross section}$$

$$\langle \sigma v \rangle = 2\pi Z_i e \left(\frac{\alpha_n}{\mu_{in}} \right)^{1/2} \equiv k_L \approx 10^{-9} \text{ cm}^3 \text{ s}^{-1} \text{ independent on } T$$

Orbits in r^{-4} potential



- If $b < b_0$ reactive collision
- If $b > b_0$ deflection (ion-neutral momentum transfer)

Reaction cross section:

$$\sigma = 2\pi \int_0^{b_0} b \, db = \pi b_0^2 = 2\pi Z_i e \left(\frac{\alpha_n}{\mu_{in}} \right)^{1/2} \frac{1}{v}$$

This is the Langevin cross section. The Langevin rate is

$$\langle \sigma v \rangle = 2\pi Z_i e \left(\frac{\alpha_n}{\mu_{in}} \right)^{1/2} \equiv k_L \quad \text{independent on } T$$

Numerical value, with $\alpha \approx 1 \text{ \AA}^3$, $\mu_{in} \approx m_H$:

$$k_L \approx 10^{-9} \text{ cm}^3 \text{ s}^{-1}$$

Example: $\text{H}_2^+ + \text{H}_2 \rightarrow \text{H}_3^+ + \text{H}$

- a “cornerstone” reaction in molecular clouds:
 H_2 ionized by photons, CRs, X-rays, reacts with ambient H_2

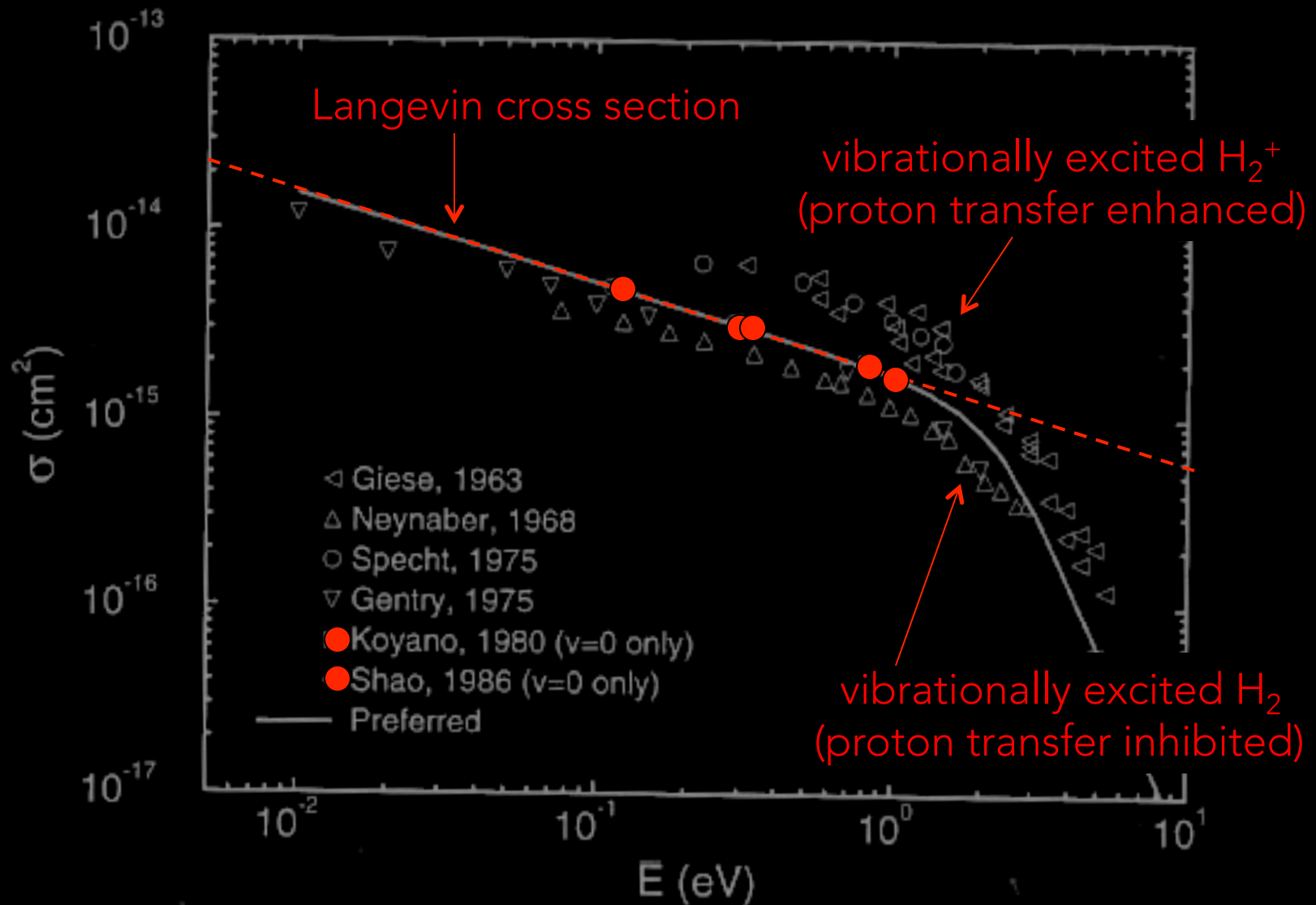
May proceed by proton transfer:



and atom transfer

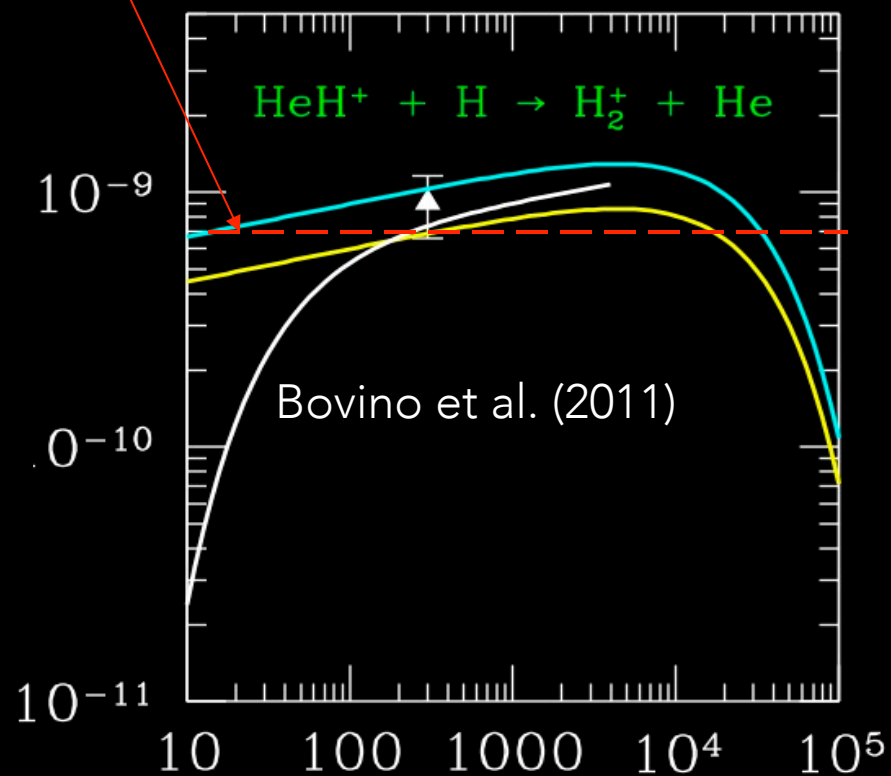
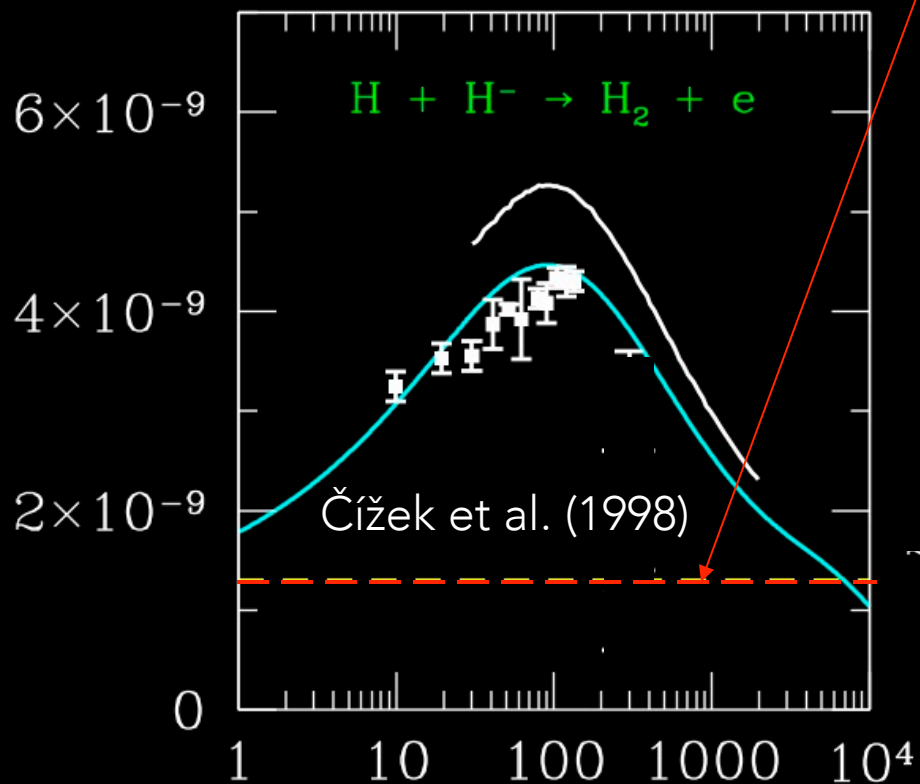


- If both H_2 and H_2^+ are in their $v=0$, proton transfer dominates.
- Otherwise, it depends.



Linder, Janev & Botero (1995)

Langevin rate



Momentum transfer cross section

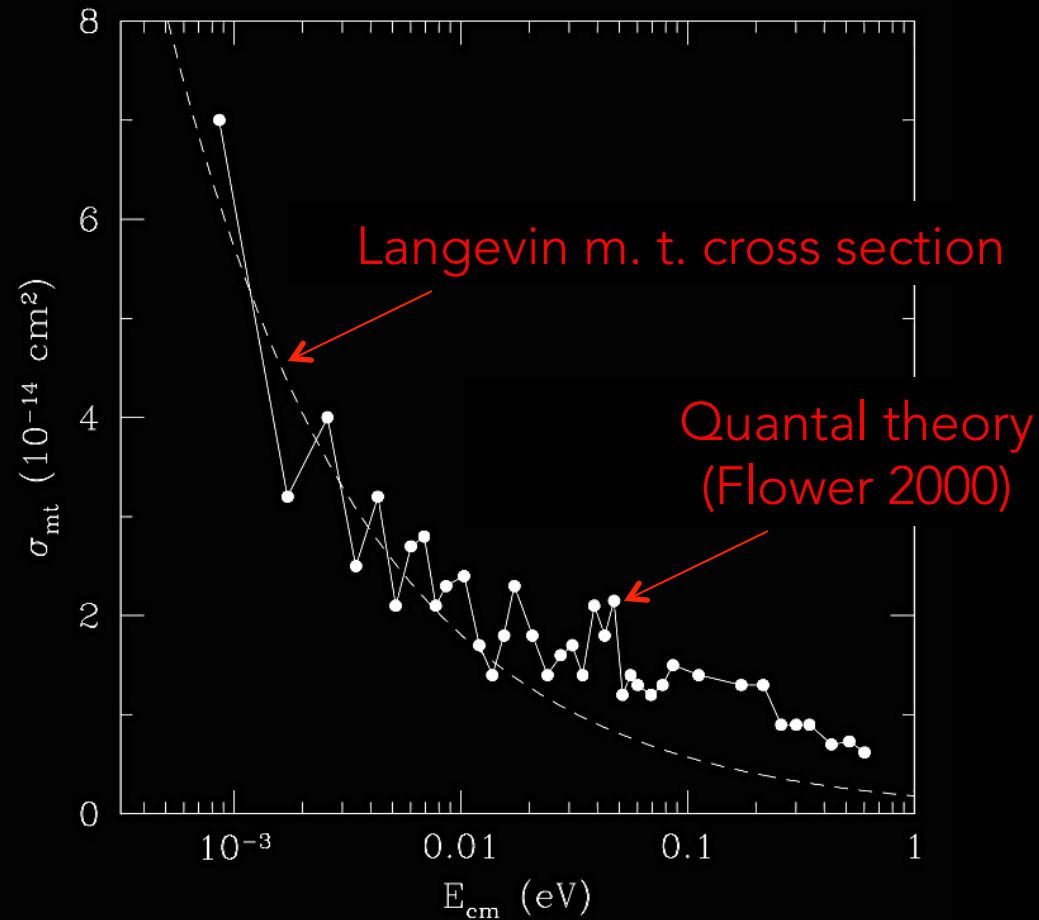
- elastic (i.e. non-reactive) collisions
- momentum exchange between ions and neutrals
- important for MHD codes

$$\sigma_{mt} = 2\pi \int_{b_0}^{\infty} (1 - \cos \theta) b \, db = 2.21\pi Z_i e \left(\frac{\alpha_n}{\mu_{in}} \right)^{1/2} \frac{1}{v}$$

where $\theta(b)$ = scattering angle. Only 1.105 times Langevin c.s.

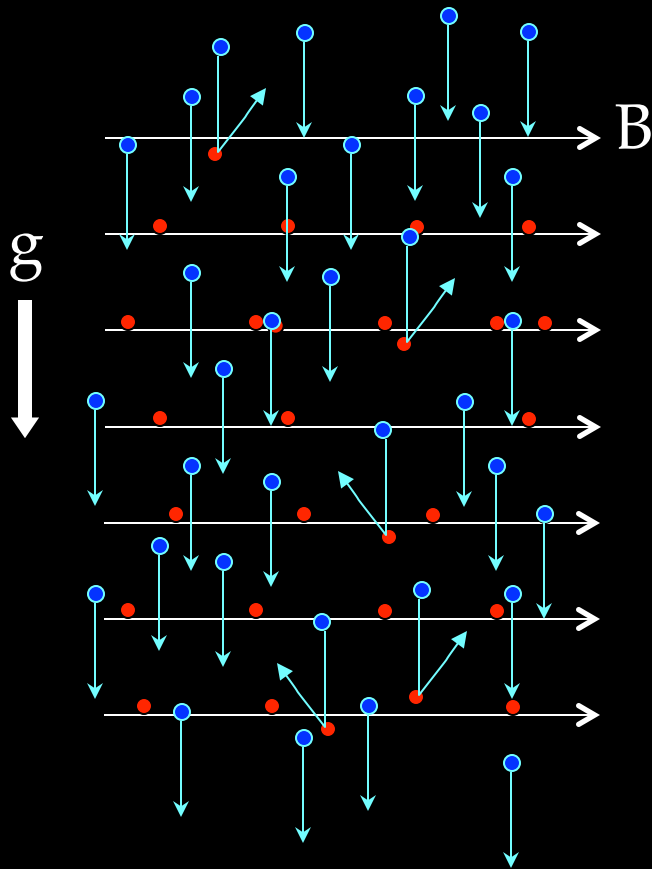
- Contribution of $b < b_0$ can be included assuming orbiting collisions result in isotropic scattering with $\langle \cos \theta \rangle = 0$:
factor 2.21 \rightarrow 2.41

Example: $\text{HCO}^+ + \text{H}_2$ momentum transfer



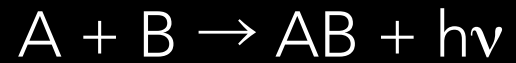
Ambipolar diffusion

- neutrals
- ions, electrons



- The field acts on neutrals indirectly through collisions between neutral and charged particles: frictional force mediated by momentum-transfer collisions.
- The field and the ions slip through the neutrals (ion-slip or ambipolar diffusion);
- The momentum-transfer cross section ion-neutrals controls the process.

2. Radiative association

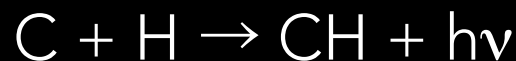


- Collision product stabilized through photon emission
- $t_{\text{collision}} \approx a_0/v \approx 10^{-13} \text{ s}$ if $v=0.5 \text{ km s}^{-1}$
- $t_{\text{radiative}} \approx A_{\text{ul}}^{-1} \approx 10^{-7} \text{ s}$ dipole electronic transition

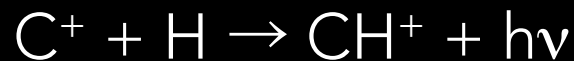
$$\sigma \approx (\pi a_0^2) (t_{\text{collision}}/t_{\text{radiative}}) \approx 10^{-6} a_0^2$$

$$k_{\text{rad. ass.}} = \langle \sigma v \rangle \approx 10^{-17} \text{ cm}^3 \text{ s}^{-1}$$

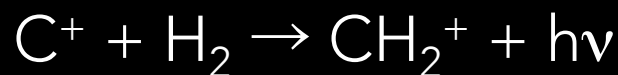
- Generally slow, independent on T. Needs large dipole moments because $A_{\text{ul}} \sim d^2$



$$k_{\text{rad. ass.}} = 1.0 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$$



$$k_{\text{rad. ass.}} = 1.7 \times 10^{-17} \text{ cm}^3 \text{ s}^{-1}$$



$$k_{\text{rad. ass.}} = 6.0 \times 10^{-16} \text{ cm}^3 \text{ s}^{-1}$$

- Semiclassical estimates of radiative association rate for primordial molecules (Lepp & Shull 1984):

$$\text{H}_2 \text{ (d=0)} \rightarrow k_{\text{H}_2} \approx 0$$

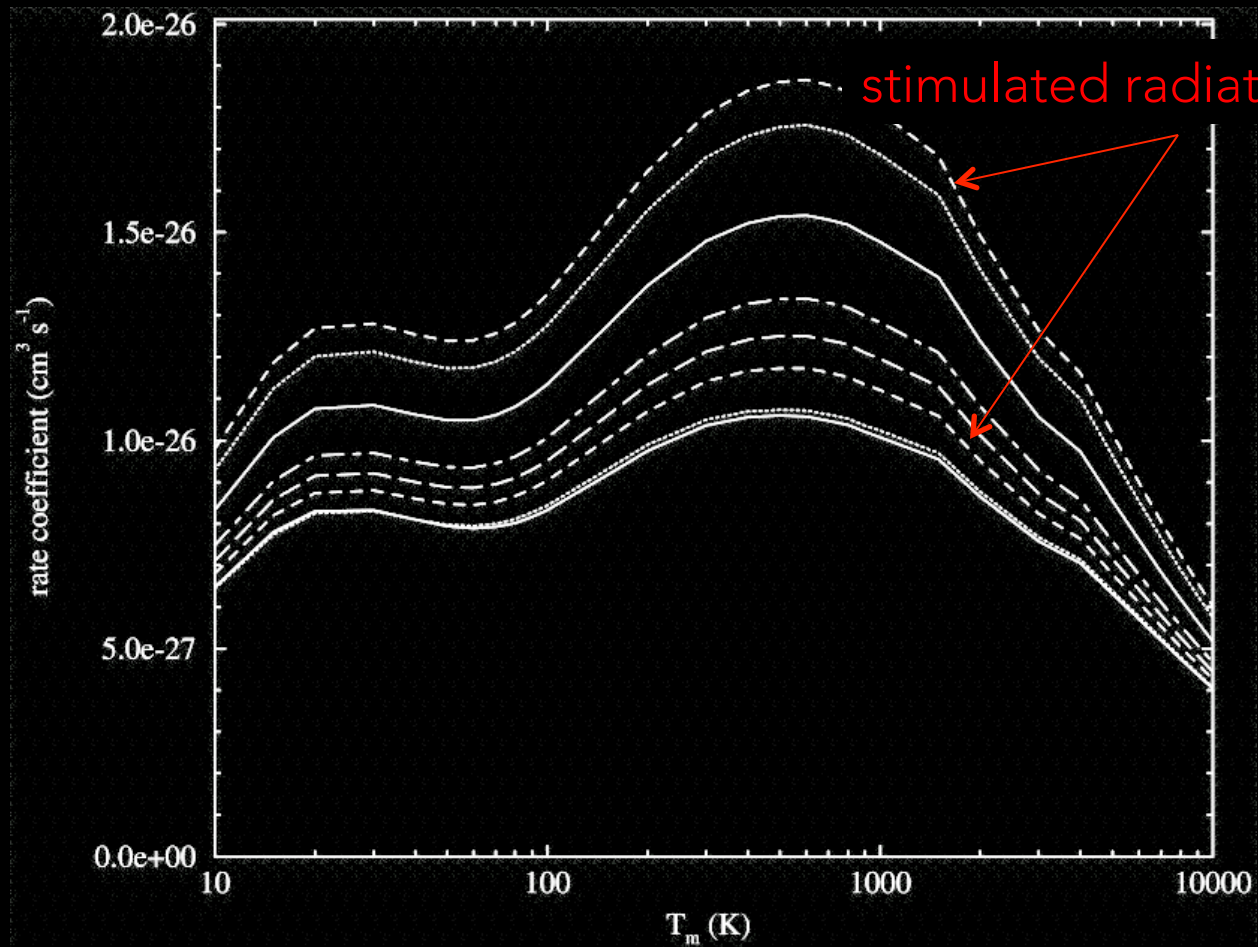
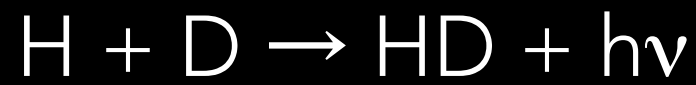
$$\text{HD (d=6x10}^{-4} \text{ debyes)} \rightarrow k_{\text{HD}} \approx 10^{-25} \text{ cm}^3 \text{ s}^{-1}$$

$$\text{LiH (d=6 debyes)} \rightarrow k_{\text{LiH}} \approx 10^{-17} \text{ cm}^3 \text{ s}^{-1}$$

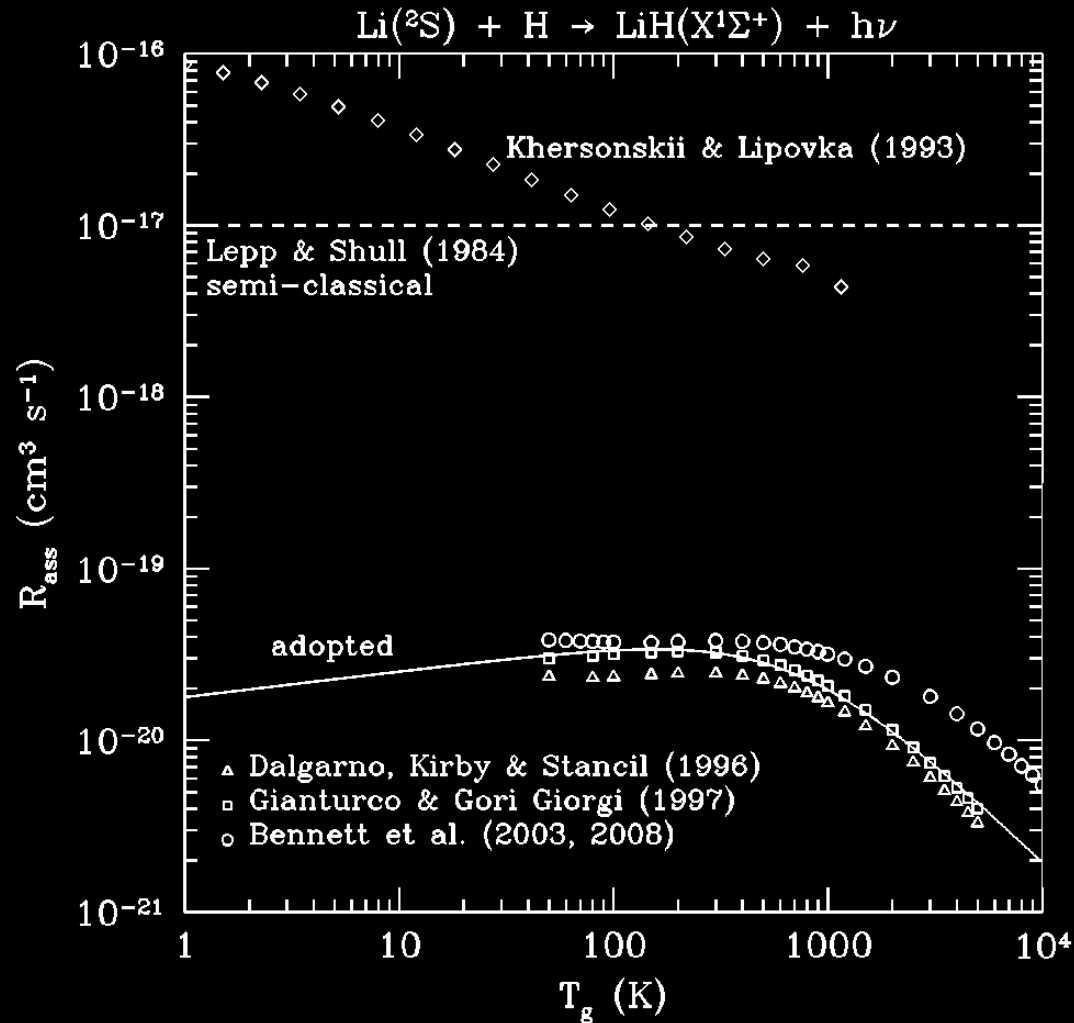
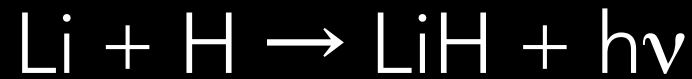
- Warning: semiclassical results can be overestimated!
- Fully quantal calculations:

$$k_{\text{HD}} \approx 10^{-26} \text{ cm}^3 \text{ s}^{-1} \quad (\text{Stancil \& Dalgarno 1997})$$

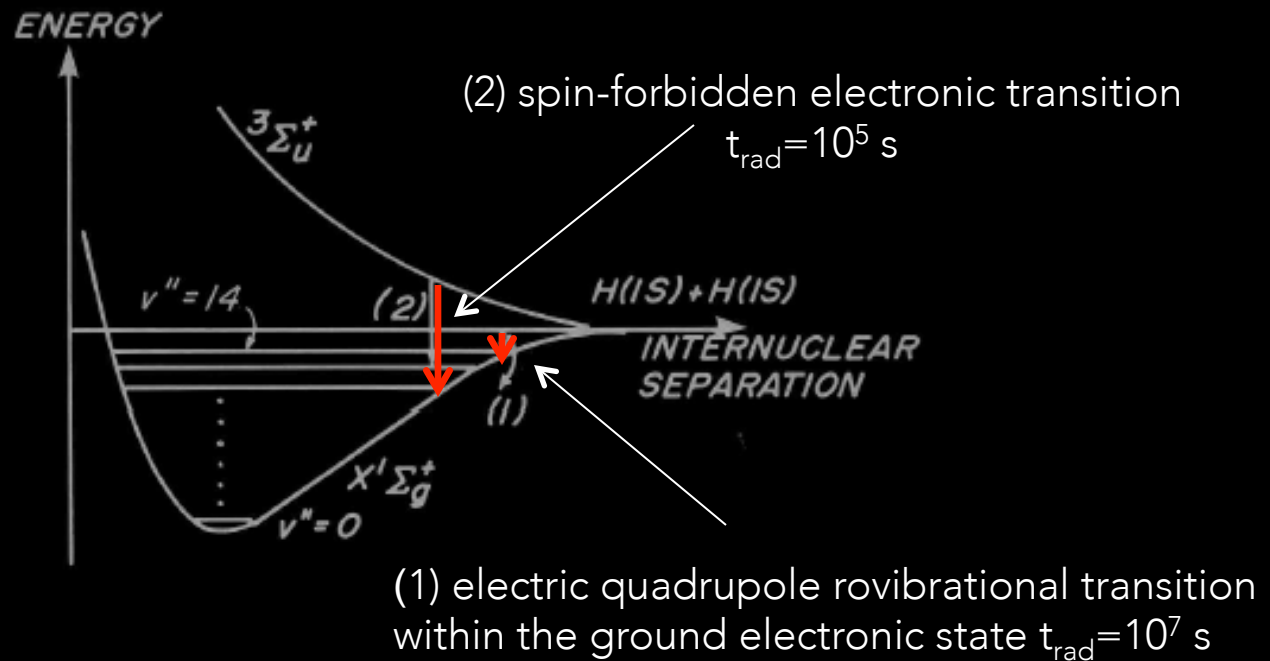
$$k_{\text{LiH}} \approx 10^{-20} \text{ cm}^3 \text{ s}^{-1} \quad (\text{Dalgarno et al. 1996})$$



Stancil & Dalgarno (1997)

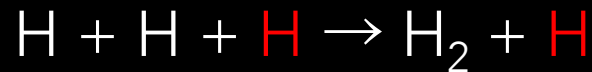


- Does not work for $\text{H} + \text{H} \rightarrow \text{H}_2 + h\nu$



- (1) $k_{\text{rad. ass.}} = 10^{-31} \text{ cm}^3 \text{ s}^{-1}$ (2) $k_{\text{rad. ass.}} = 10^{-29} \text{ cm}^3 \text{ s}^{-1}$

- Needs a third body to remove excess energy that cannot be radiated away



rate $k \approx 5.5 \times 10^{-29} (\text{T}/^\circ\text{K})^{-1} \text{ cm}^6 \text{ s}^{-1}$ (uncertain)

important only at high density ($n > 10^8 \text{ cm}^{-3}$)

- Or a catalyst (dust grain): $\text{H} + \text{H} \rightarrow \text{H}_2$

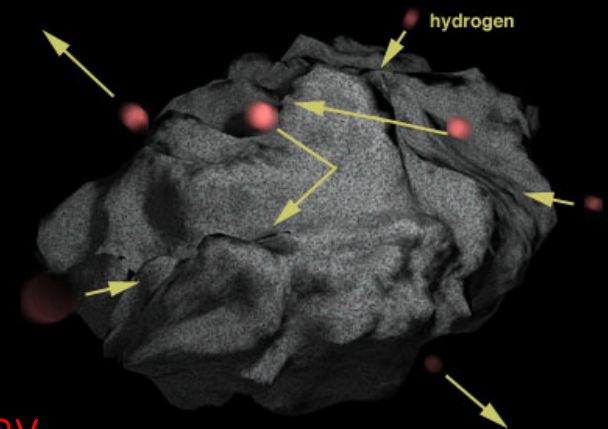
$$\frac{dn_{\text{H}_2}}{dt} = k n_{\text{H}} n_{\text{g}} \quad k = \frac{1}{2} (\pi a^2) v S \gamma$$

v = speed of H atoms in gas-phase

a = grain radius

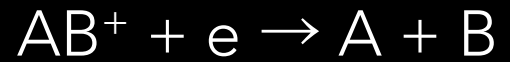
S = sticking probability

γ = surface reaction probability

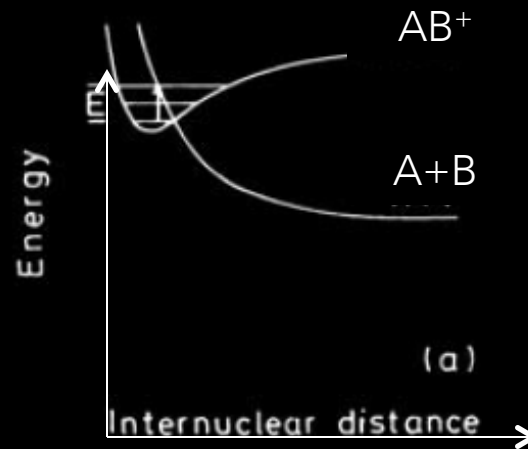


→ see talks by W.-F. Thi and T. Grassi on friday

3. Dissociative recombination

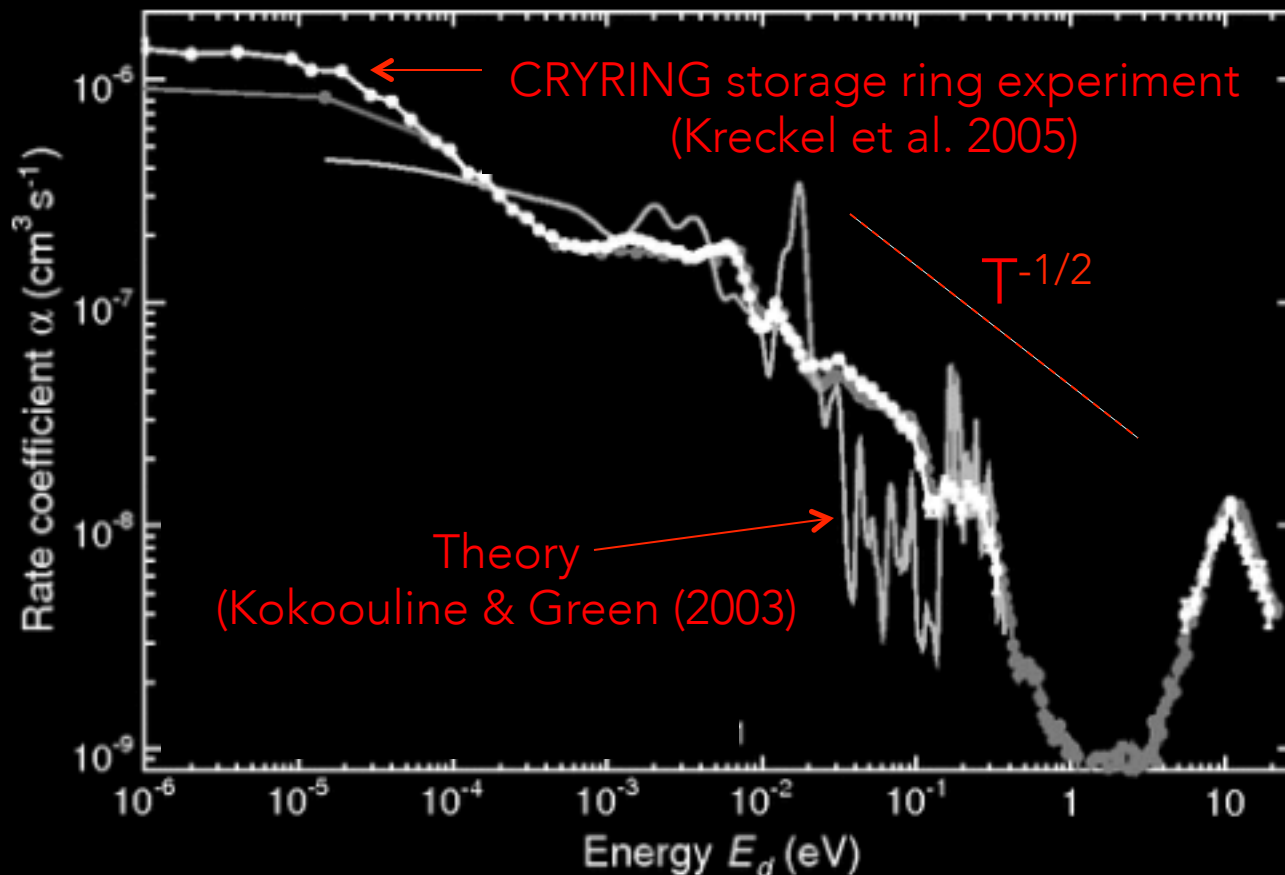
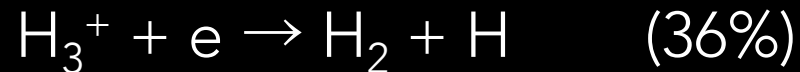


- Electron excites transition of stable AB^+ ion to a repulsive state of AB molecule which crosses the energy curve of the ion.



- Example: $HCO^+ + e \rightarrow H + CO$ (important CO source)
- Theoretically complex, experimentally difficult
- Large rate coefficient: $10^{-7} - 10^{-6} \text{ cm}^3 \text{ s}^{-1}$ at $T=10 \text{ K}$ proportional to $T^{-1/2}$ for a Maxwellian distribution

Dissociative recombination of H_3^+



4. Neutral-neutral reactions



- if $b < R_1 + R_2 \approx \text{a few } a_0$ ("hard-sphere" model)
 $\sigma = \pi(R_1 + R_2)^2 \approx 10^{-15} \text{ cm}^2$
 $\langle \sigma v \rangle = \pi(R_1 + R_2)^2 \left(\frac{8kT}{\pi \mu_{mn}} \right)^{1/2} \approx 10^{-10} \text{ cm}^3 \text{ s}^{-1} \text{ at } T=10 \text{ K}$
- Correction for attractive Van der Waals forces at larger b (fluctuations in the dipole of one species induce a dipole in the other)

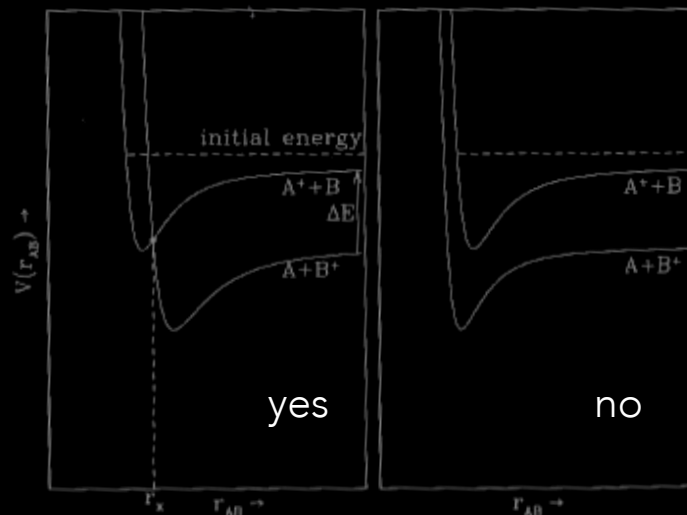
$$V_{nm}(r) = -\frac{\alpha_n \alpha_m}{r^6} I_{nm} \quad I_{nm} = \langle I_n + I_m \rangle$$

$$\langle \sigma v \rangle = 13.5\pi \left[\frac{\alpha_n \alpha_m I_{nm}}{\mu_{mn}} \left(\frac{8kT}{\pi \mu_{mn}} \right)^{1/2} \right]^{1/3} \approx 10^{-11} \left(\frac{T}{100 \text{ K}} \right)^{1/6} \text{ cm}^3 \text{ s}^{-1}$$

5. Charge transfer reactions



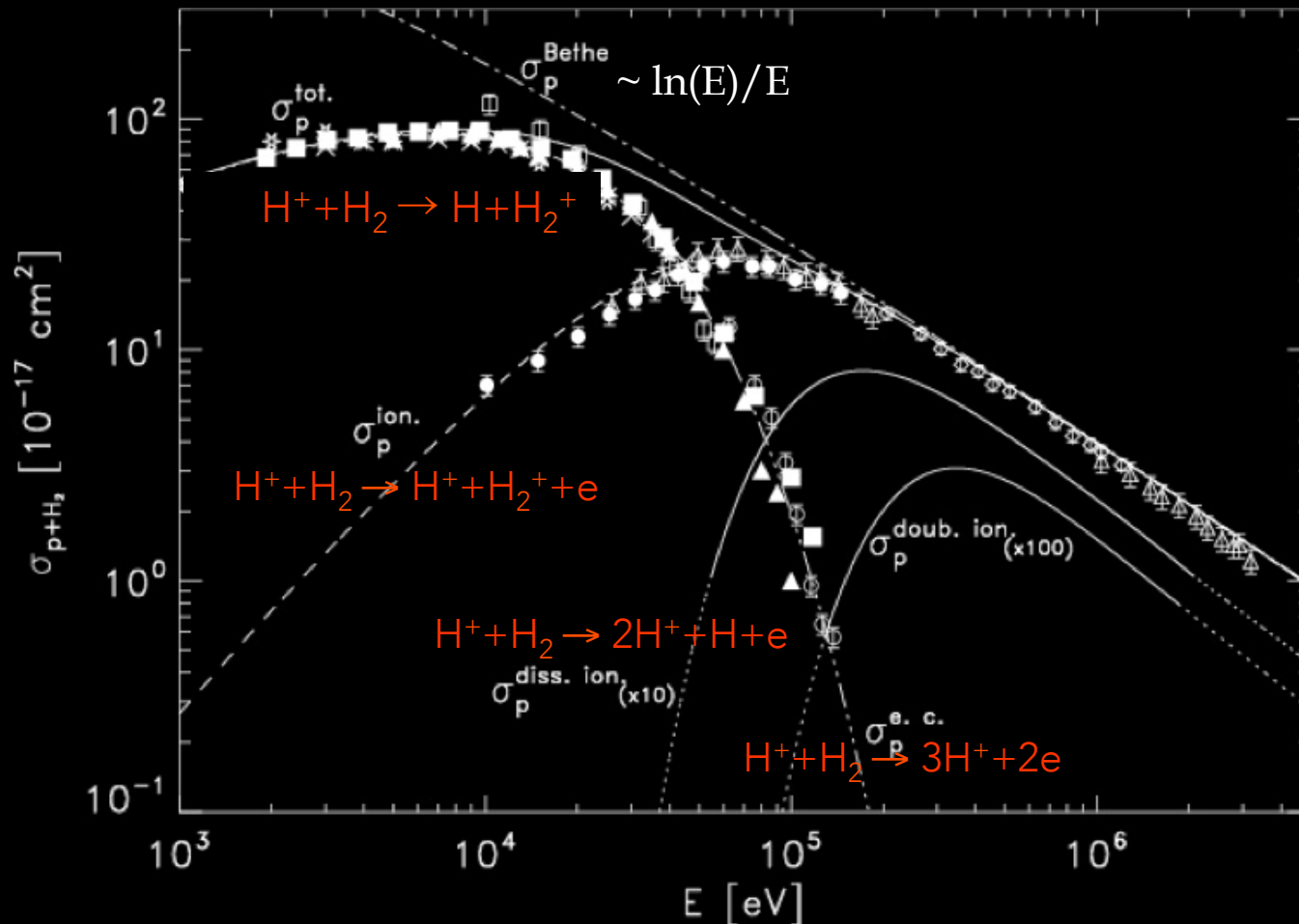
- $t_{\text{collision}} = a_0/v \approx 10^{-13} \text{ s}$ if $v \approx 0.5 \text{ km s}^{-1}$
- $t_{\text{electron transfer}} = h/\Delta E \approx 10^{-15} \text{ s}$ if $\Delta E \approx I_A - I_B \approx 1 \text{ eV}$ (released)
- Requires exothermicity and "level crossing": potential energy curves of $A^+ + B$ and $A + B^+$ must intersect.
- Reaction rate fast $k = 10^{-9} \text{ cm}^3 \text{ s}^{-1}$ and independent on T



Exothermal,
level crossing

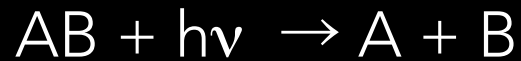
Exothermal,
no level crossing

$H^+ + H_2$: charge transfer vs. collisional ionization



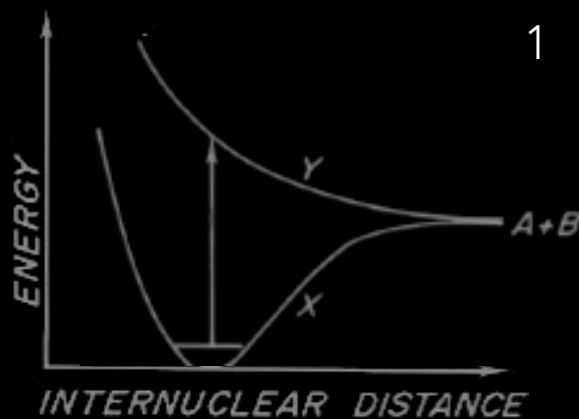
Padovani et al. (2009)

6. Photodissociation



Transition from a bound state to:

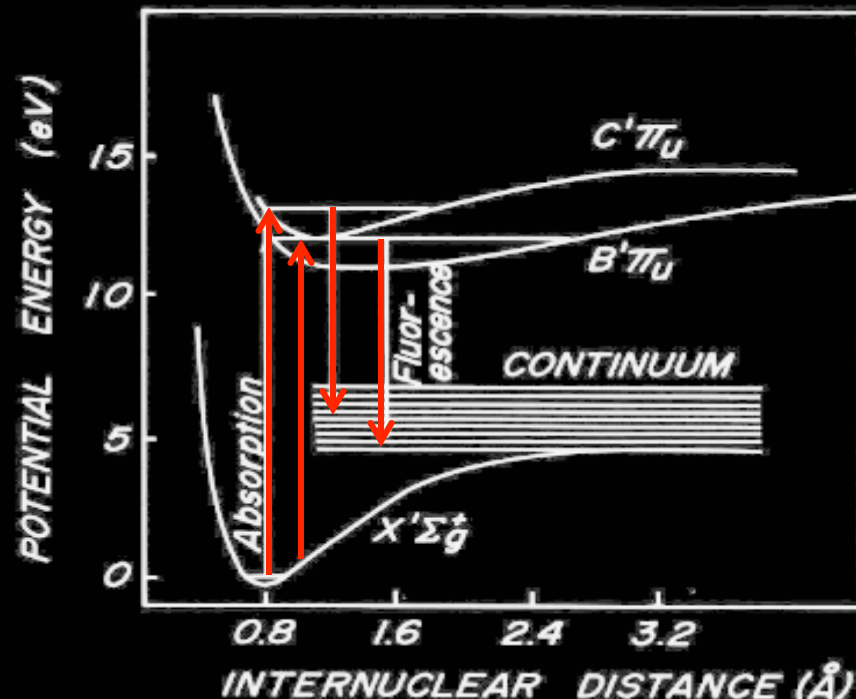
1. a repulsive state (photodissociation)
2. a bound state that decays into the continuum of the lower state by emitting a photon (two-step photodissociation)



Photodissociation of H_2 follows 2

Photodissociation of H₂

- Principal destruction process of H₂ in the ISM
- First step: absorption of a resonance line photon (E=11.2-13.6 eV) from ground state X to excited level B or C
- Second step: spontaneous decay to the vibrational continuum of X (~15% of the time), leading to dissociation.



Photodissociation rate

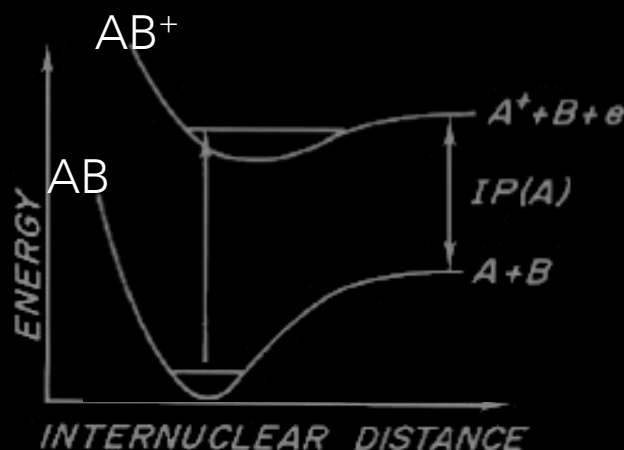
$$k_{\text{ph}} = 4\pi \int_0^\infty \frac{J(\nu)}{h\nu} \sigma_{\text{ph}}(\nu) d\nu$$

- $J(\nu)$ is the specific intensity (in $\text{erg cm}^{-2} \text{s}^{-1} \text{ster}^{-1} \text{Hz}^{-1}$)
- $\sigma_{\text{ph}}(\nu)$ is the photodissociation cross section (in cm^2)
- k_{ph} is the photodissociation rate in s^{-1}
-
- Typical values $10^{-11} (\text{H}_2) - 10^{-9} \text{s}^{-1}$ (CH , CN , O_2 , H_2CO)

7. Photoionization

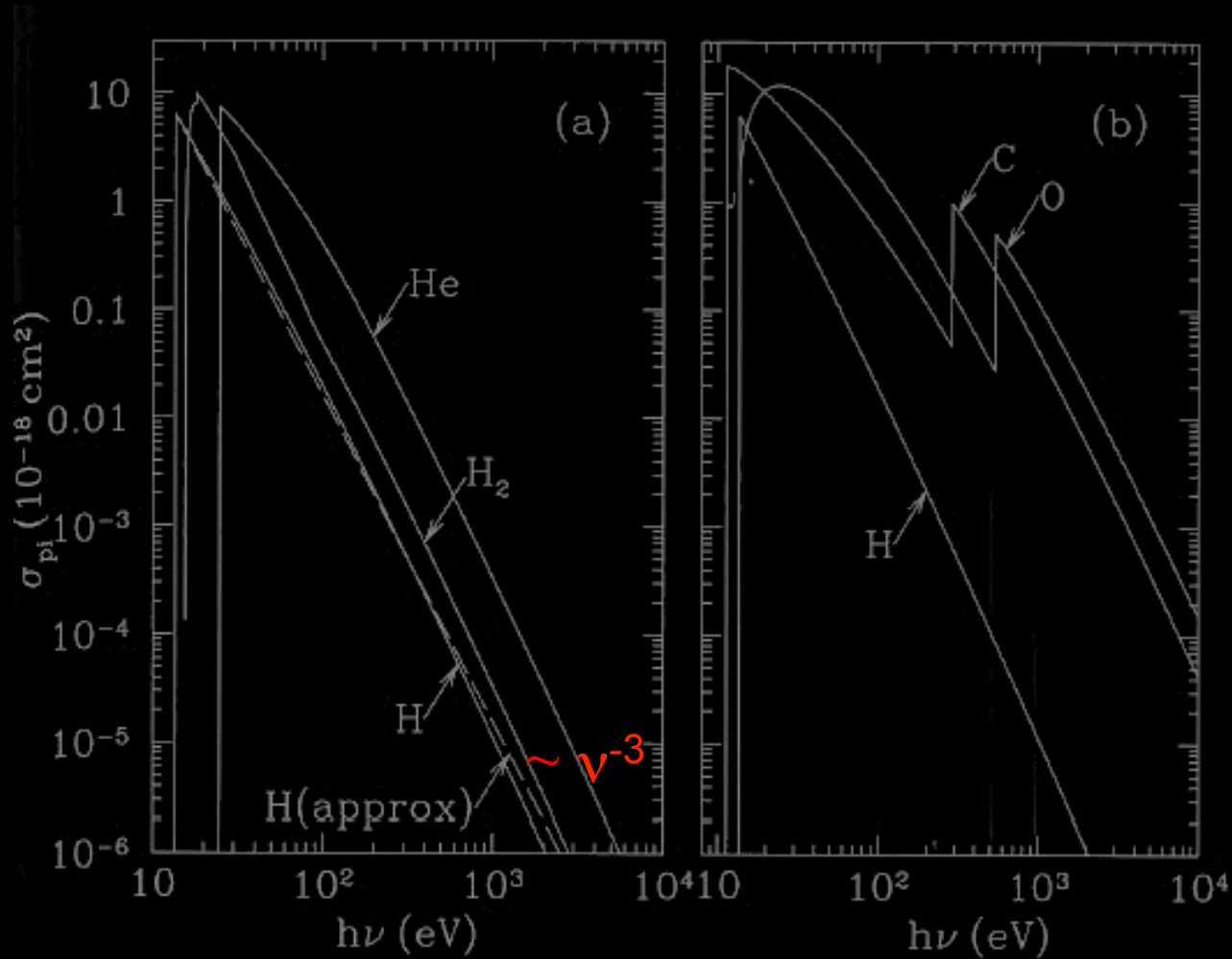


- Similar to photodissociation
- Transition from a bound state of AB to a bound state of AB^+ that lies above the $A+B$ state by the ionization potential IP



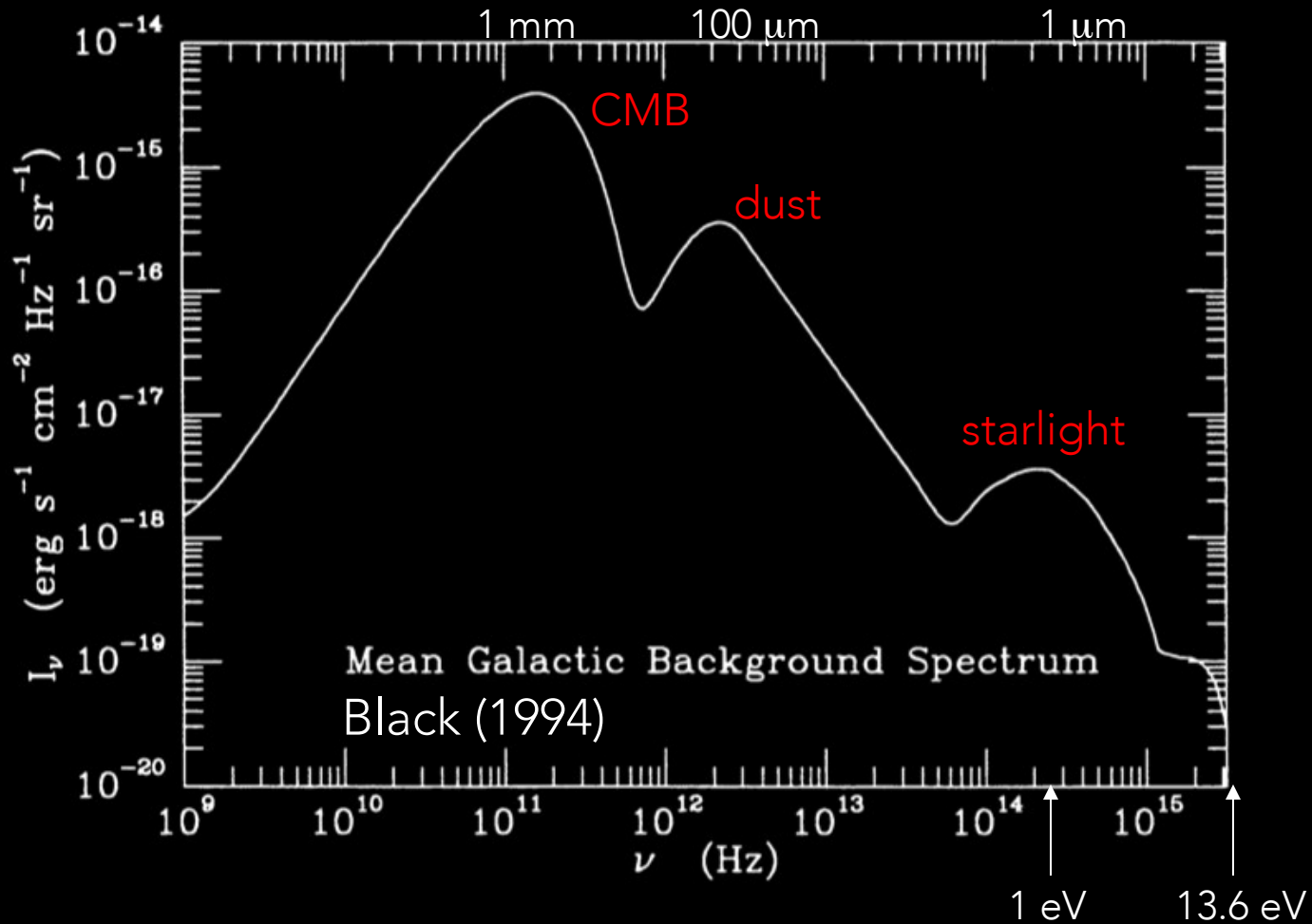
- $I_{CH}=10.64$ eV, $I_{CO}=14.01$ eV, $I_{H_2}=15.44$ eV

Photoionization cross sections

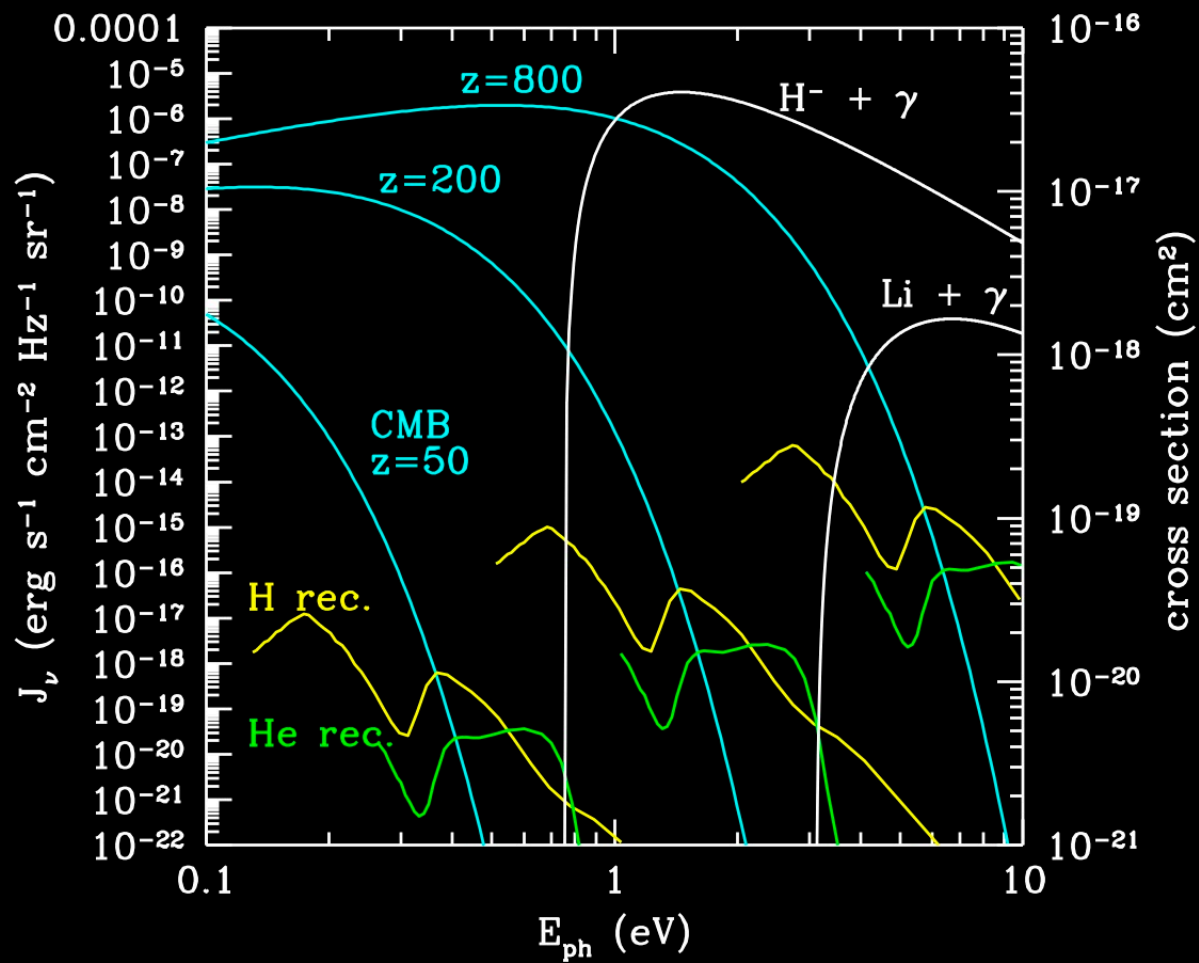


Draine (2011)

Interstellar radiation spectrum



→ see talks by W.-F. Thi and T. Grassi on wednesday



Switzer & Hirata (2005)

Hirata & Padmanabhan (2006)

Chemistry in the Early Universe

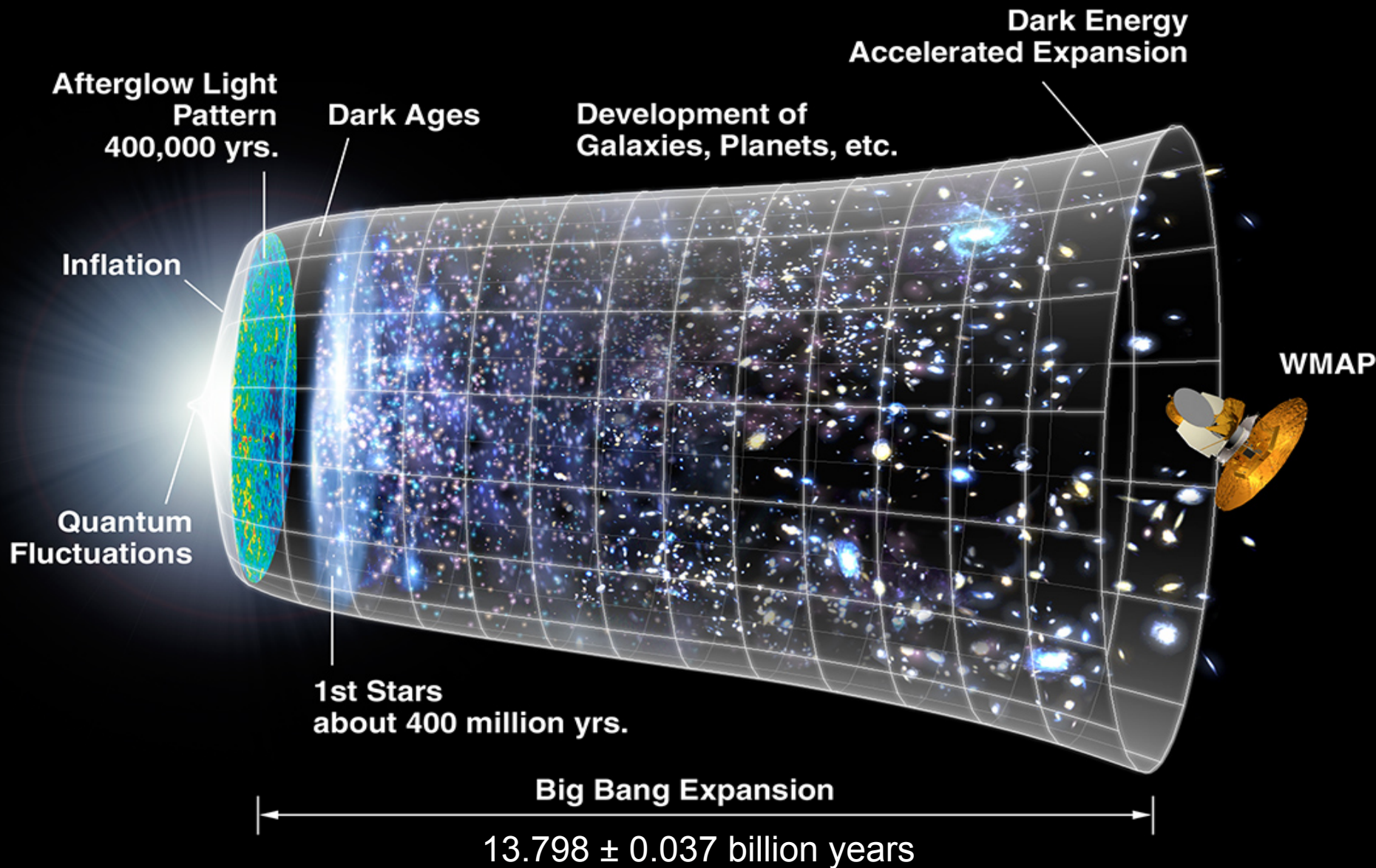
Unfavorable environment for chemical enrichment:

- rapid expansion
- strong radiation field (CMB)
- gas chemically inert ($H=0.924$, $He=0.076$, $D=2 \times 10^{-5}$, $Li=4 \times 10^{-10}$)
- no solid particles (catalyzers)

→ low molecular abundances

Main molecules and ions:

- Hydrogen subsystem: H_2 , H_2^+ , H_3^+ , H^- , H_3^+
- Deuterium " " : HD , HD^+ , H_2D^+
- Helium " " : He_2^+ , HeH^+
- Lithium " " : LiH , LiH^+ , $LiHe^+$



COBE
WMAP
PLANCK



?

LOFAR
SKA



HST



The Dark Ages

CMB
 $z \sim 1000$
400,000 yr after BB

First stars
 $z \sim 10$
400 Myr after BB

Reionization
completed
 $z \sim 7$

The cosmological background

the Dark Ages:

- start: after H recombination ($z \sim 1000$, $t \sim 400,000$ yr)
- end: formation of the first stars ($z \sim 10$, $t \sim 400$ million yr)

- Baryon density $n \approx 10^{-5} \Omega_b h^2 (1+z)^3 \text{ cm}^{-3}$

- Expansion rate $\frac{dt}{dz} \approx - \frac{10^{10} \text{ yr}}{h(1+z) \sqrt{\Omega_\Lambda + (1+z)^3 \Omega_m}}$

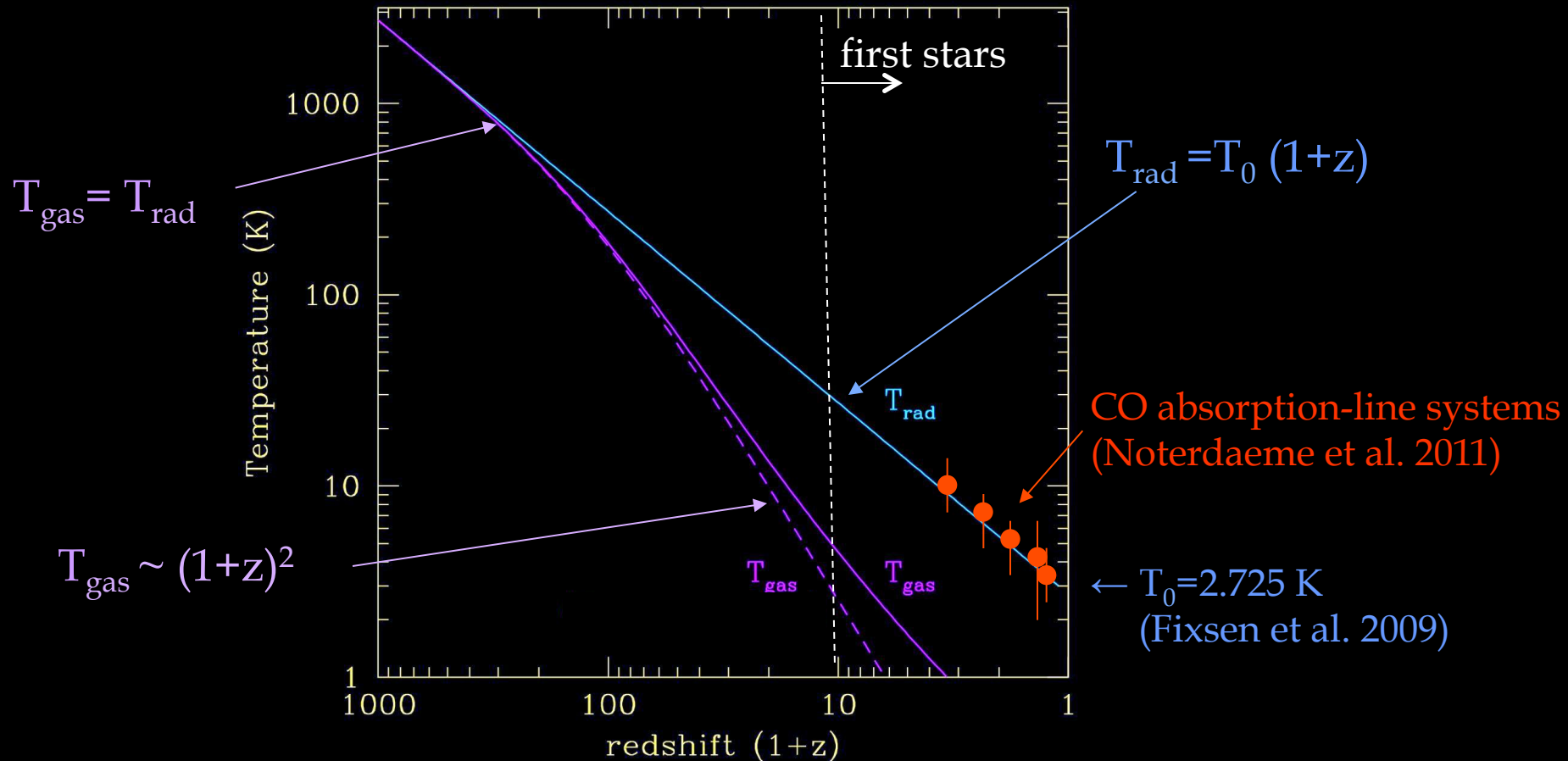
- Radiation field $T_r = T_0(1+z)$

- Cosmological parameters $h, \Omega_b, \Omega_m, \Omega_\Lambda, T_0$

$$\Omega_\Lambda = 0.726^{+0.013}_{-0.017} \quad 100 \Omega_b h^2 = 2.233^{+0.028}_{-0.038} \quad h = 0.734^{+0.072}_{-0.091} \quad T_0 = 2.726^{+0.0013}_{-0.0013} \text{ K}$$

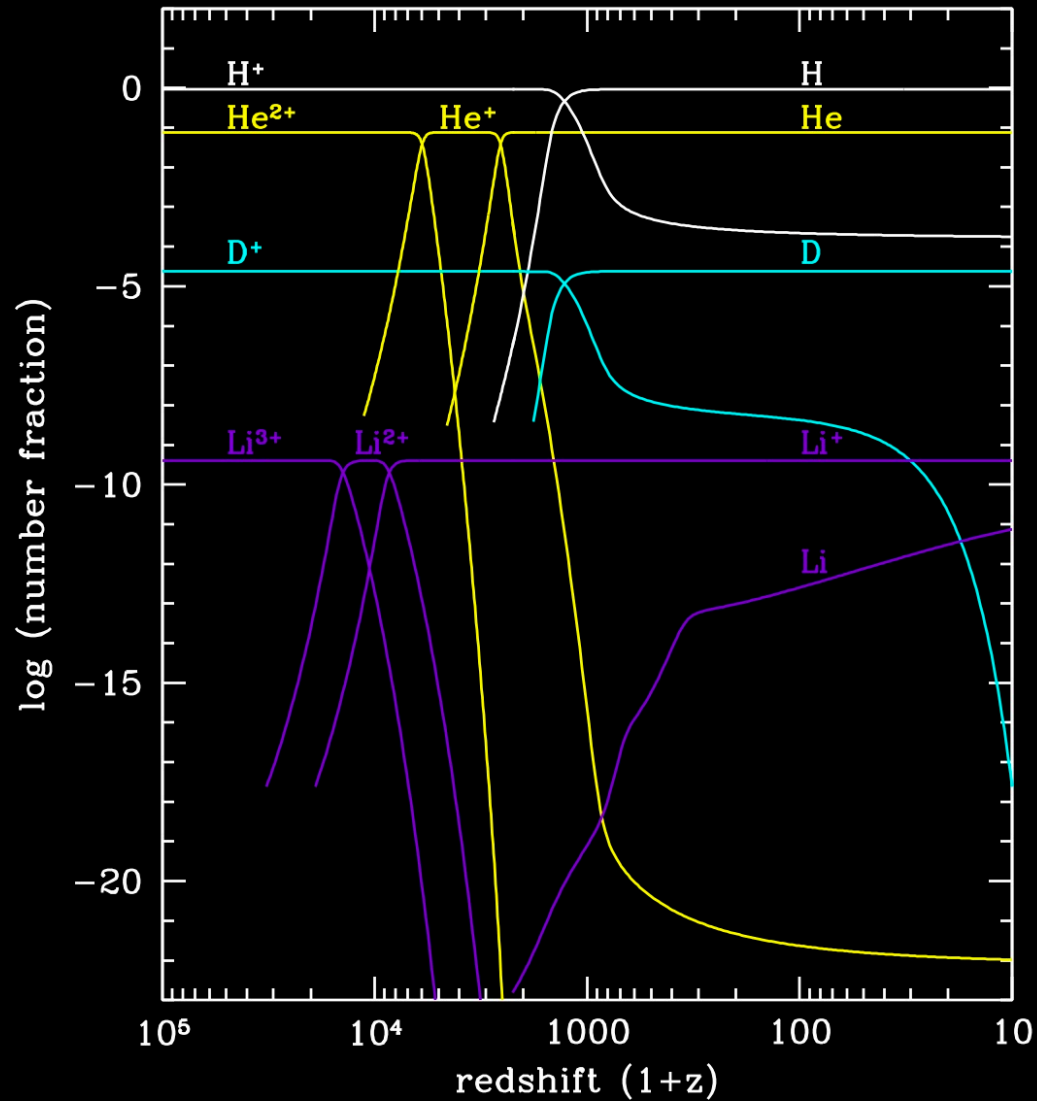
Spiegel et al. (2003), Fixsen (2009)

Temperature of matter and radiation

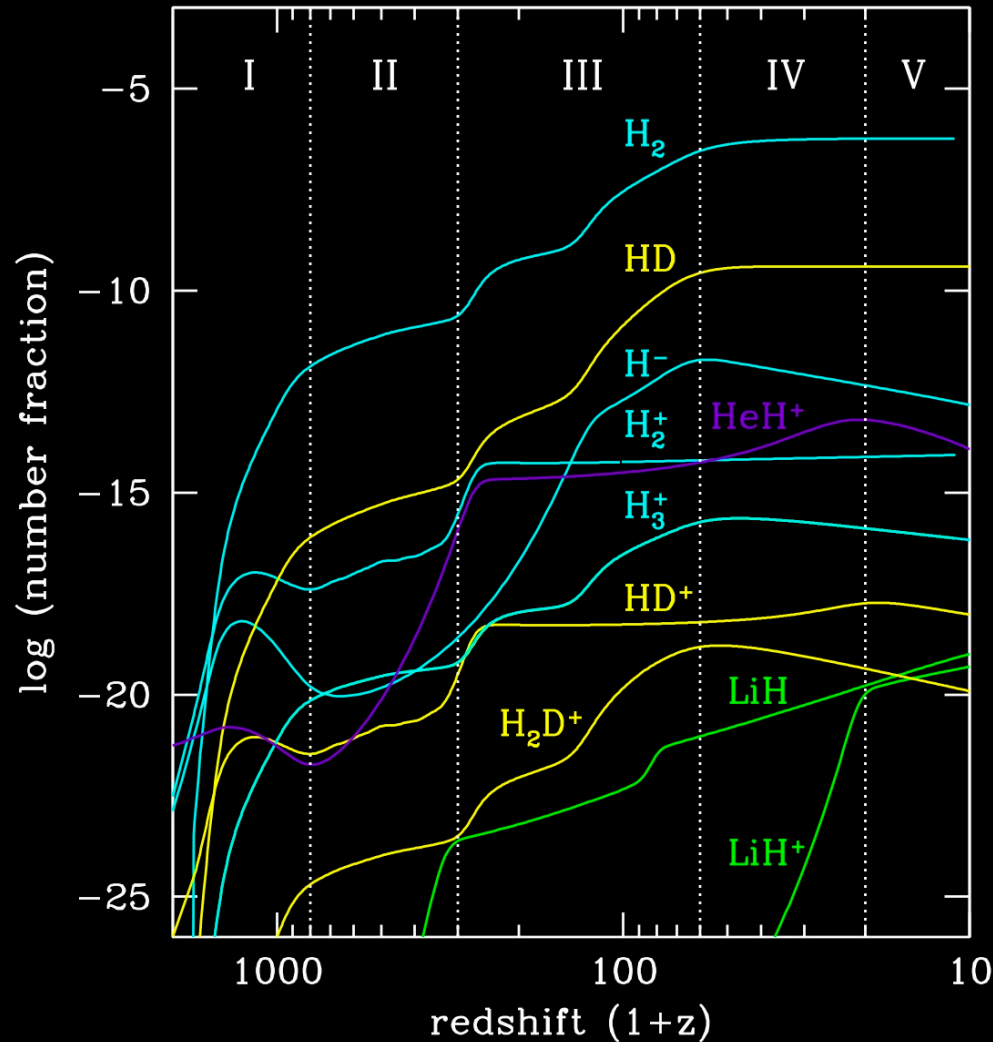


LCDM model: $h, \Omega_b, \Omega_m, \Omega_\Lambda, T_0$ from WMAP-7yr (Komatsu et al. (2011))

Ions and atoms in the Early Universe

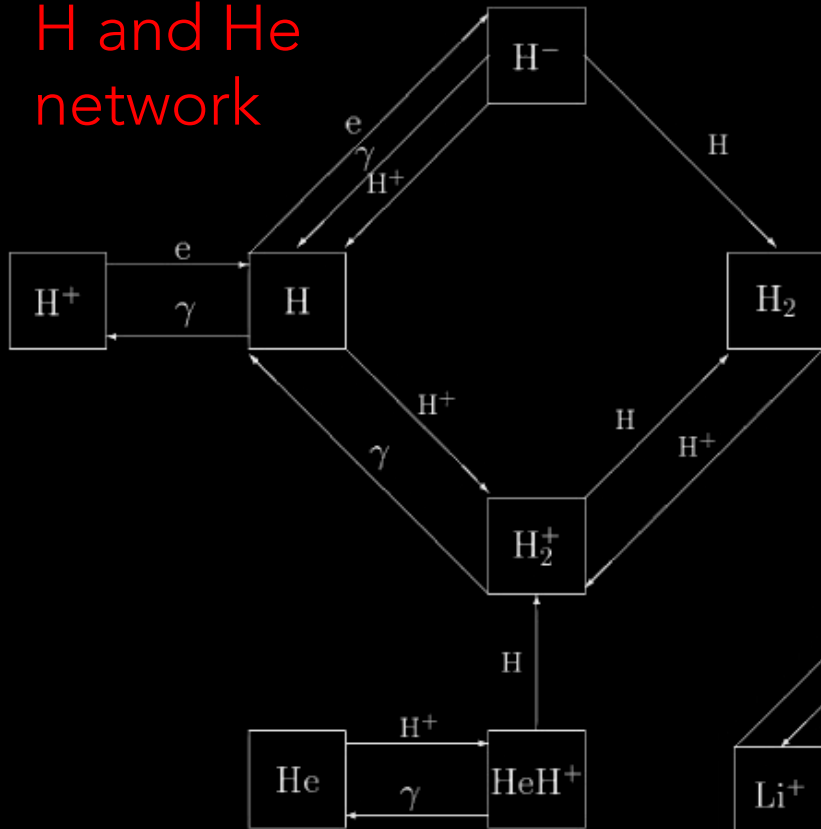


Molecules in the early Universe

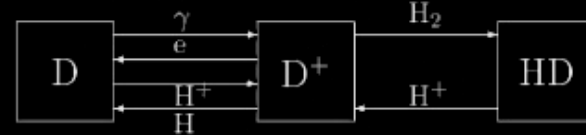


Primordial chemistry networks (simplified)

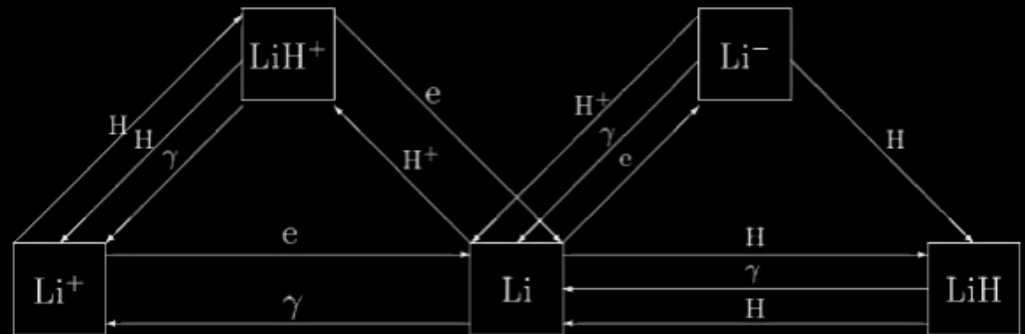
H and He
network



D network



Li network



Recent advances in primordial chemistry

Recently computed with fully quantal methods → Gianturco, Bovino et al.

- $\text{HeH}^+ + \text{H} \rightarrow \text{He} + \text{H}_2^+$
- $\text{LiH} + \text{H} \rightarrow \text{Li} + \text{H}_2$
- $\text{LiH}^+ + \text{H} \rightarrow \text{Li}^+ + \text{H}_2$
- $\text{LiH} + \text{H}^+ \rightarrow \text{Li} + \text{H}_2^+$
- $\text{LiHe}^+ + \text{H} \rightarrow \text{LiH}^+ + \text{He}$
- $\text{Li}^+ + \text{He} \rightarrow \text{LiHe}^+ + g$
- $\text{LiHe}^+ + \gamma \rightarrow \text{Li}^+ + \text{He}$
- $\text{LiHe}^+ + e \rightarrow \text{Li} + \text{He}$ (with Čurik)

Recently measured in the lab:

- $\text{H}^- + \text{H} \rightarrow \text{H}_2 + e$ **ass. det.** (Columbia Astroph. Lab., Kreckel et al. 2010)
- $\text{H}_3^+ + e \rightarrow 3\text{H}$ and $\text{H}_2 + \text{H}$ **diss. rec.** (CRYRING, TSR, McCall et al. 2004)

In progress:

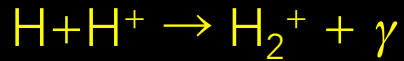
- $\text{H}^- + \text{H}^+ \rightarrow \text{H} + \text{H}$ **mut. neutr.** (DESIREE - Manne Siegbahn Lab. Stockholm)

Still uncertain:

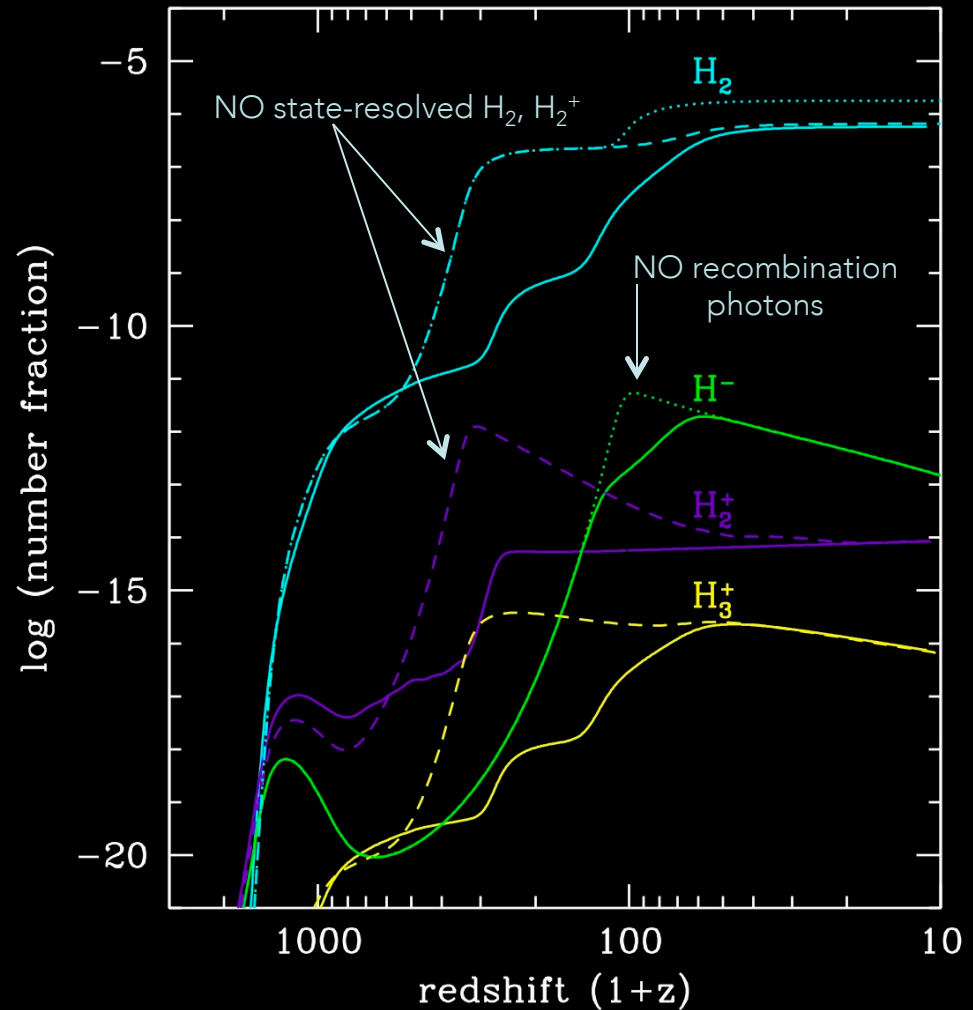
- $\text{H} + \text{H} + \text{H} \rightarrow \text{H}_2 + \text{H}$ **three-body reaction** (Bovino, Schleicher & Grassi 2014)

Hydrogen chemistry

H_2^+ channel



H^- channel



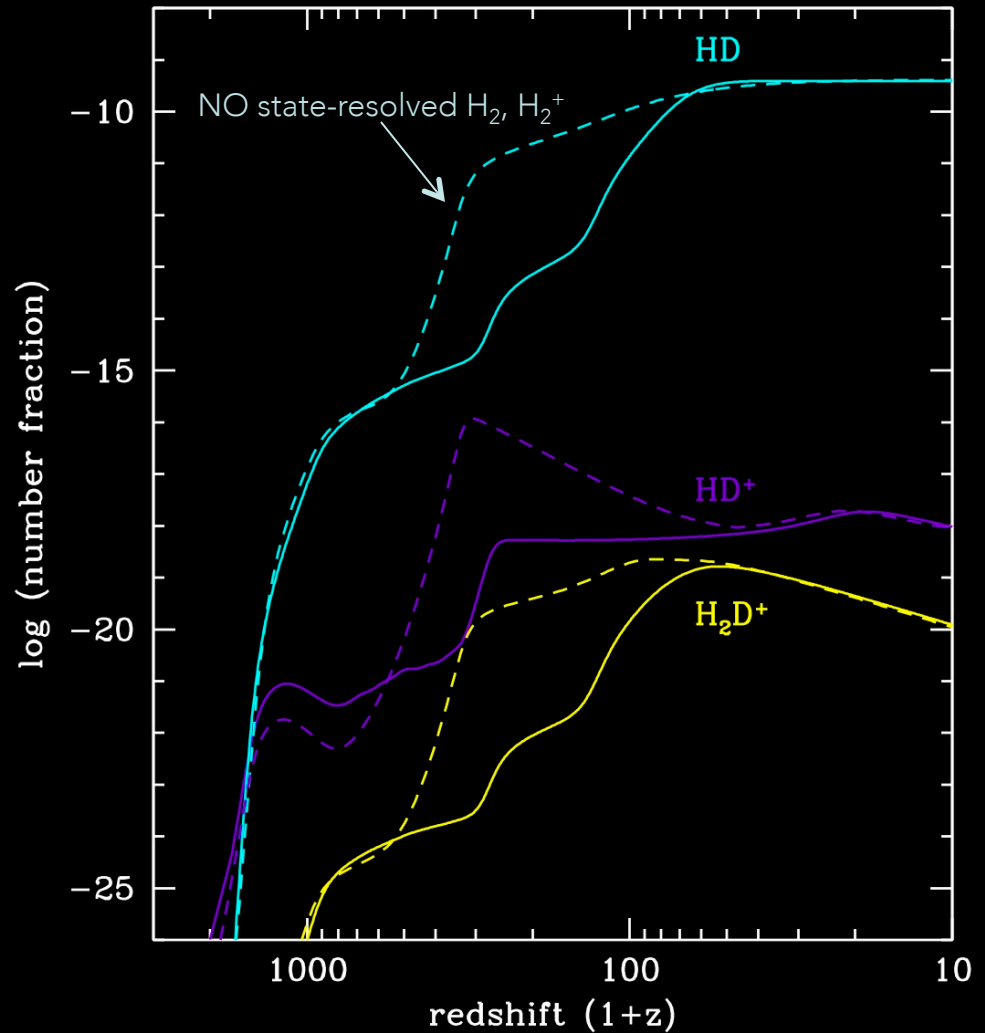
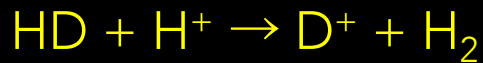
Galli & Palla (1998), Coppola et al. (2011)

Deuterium chemistry

Formation of HD:



Destruction of HD:



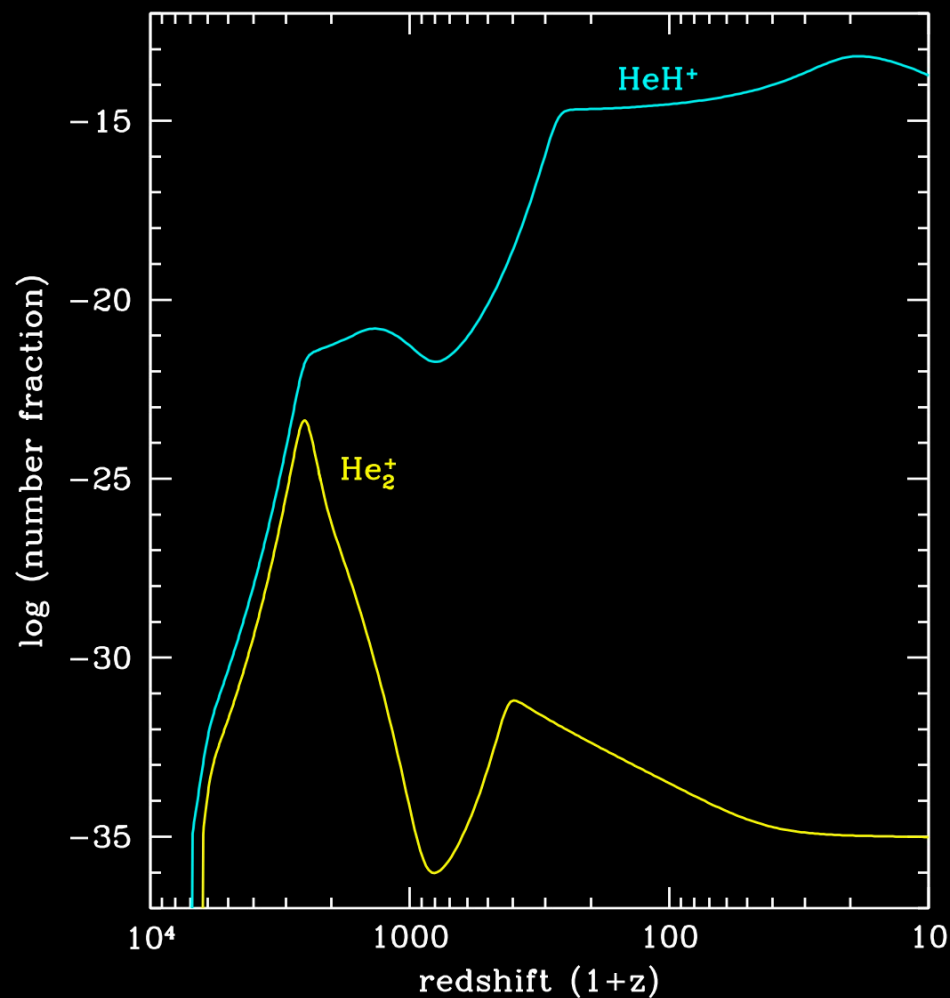
Stancil et al. (1998), Galli & Palla (2002)

Helium chemistry

Formation:



Destruction:

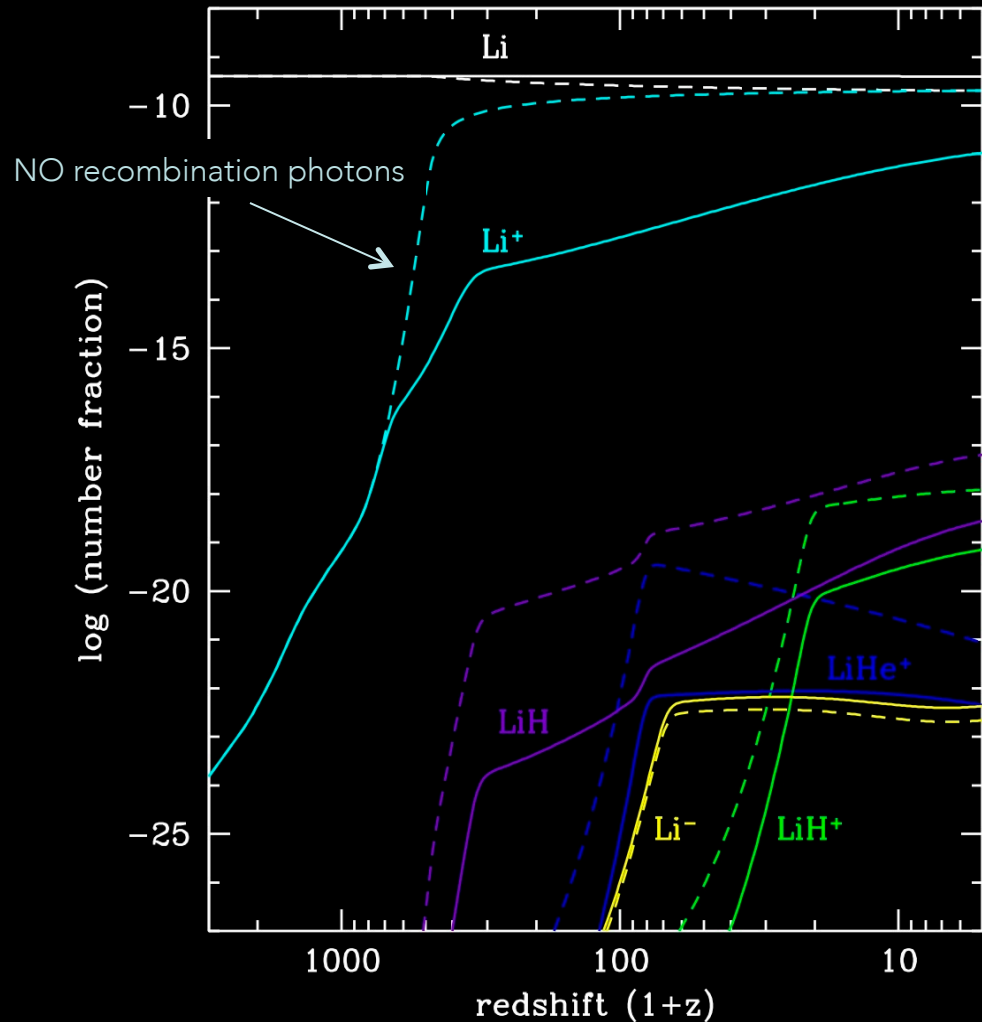
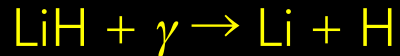


Lithium chemistry

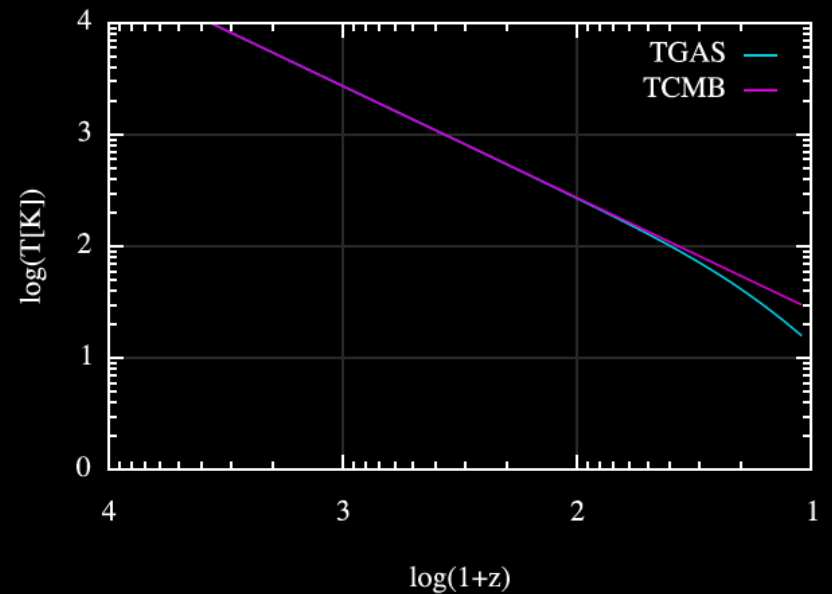
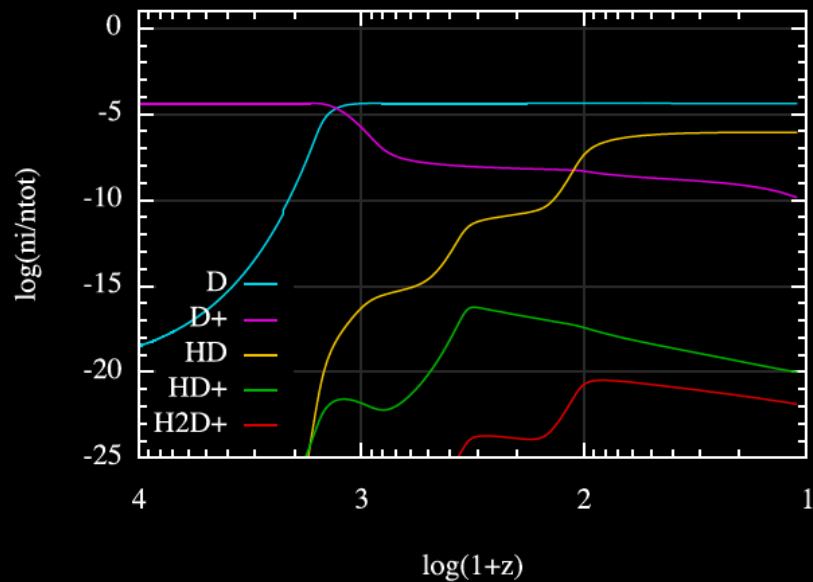
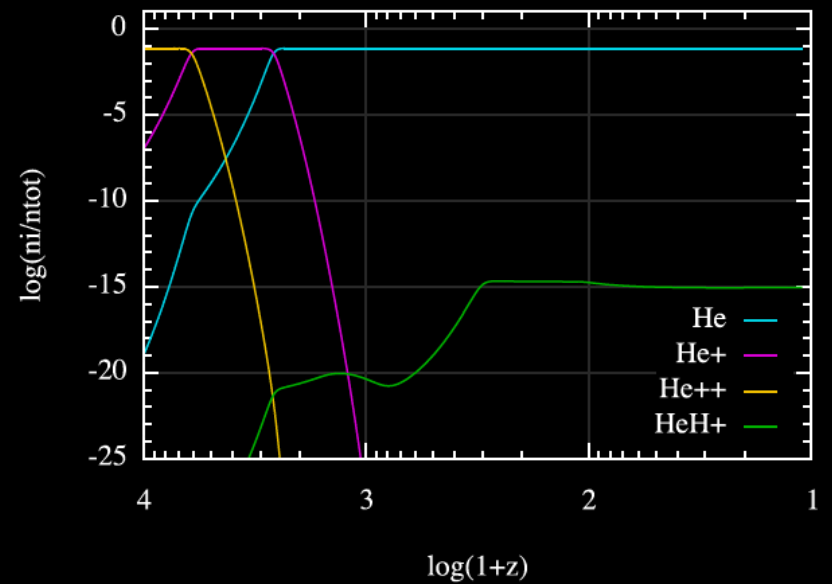
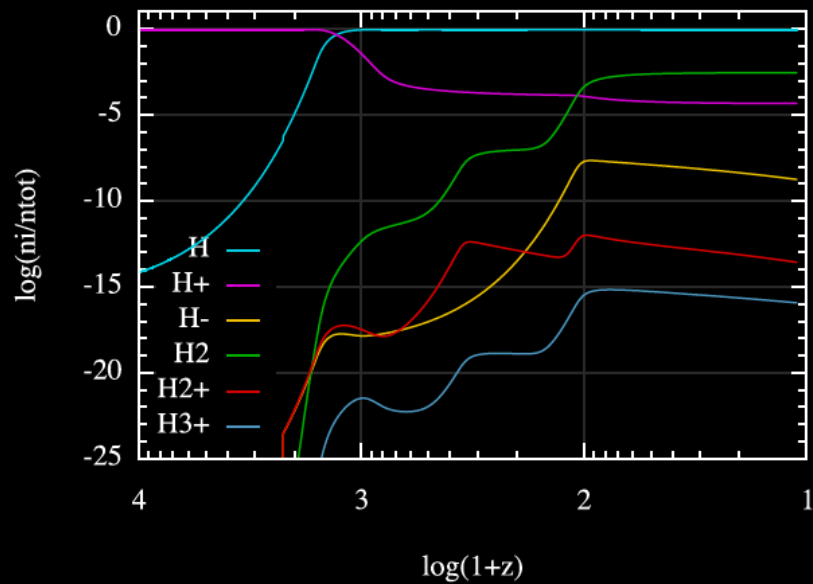
Formation of LiH:



Destruction of LiH:

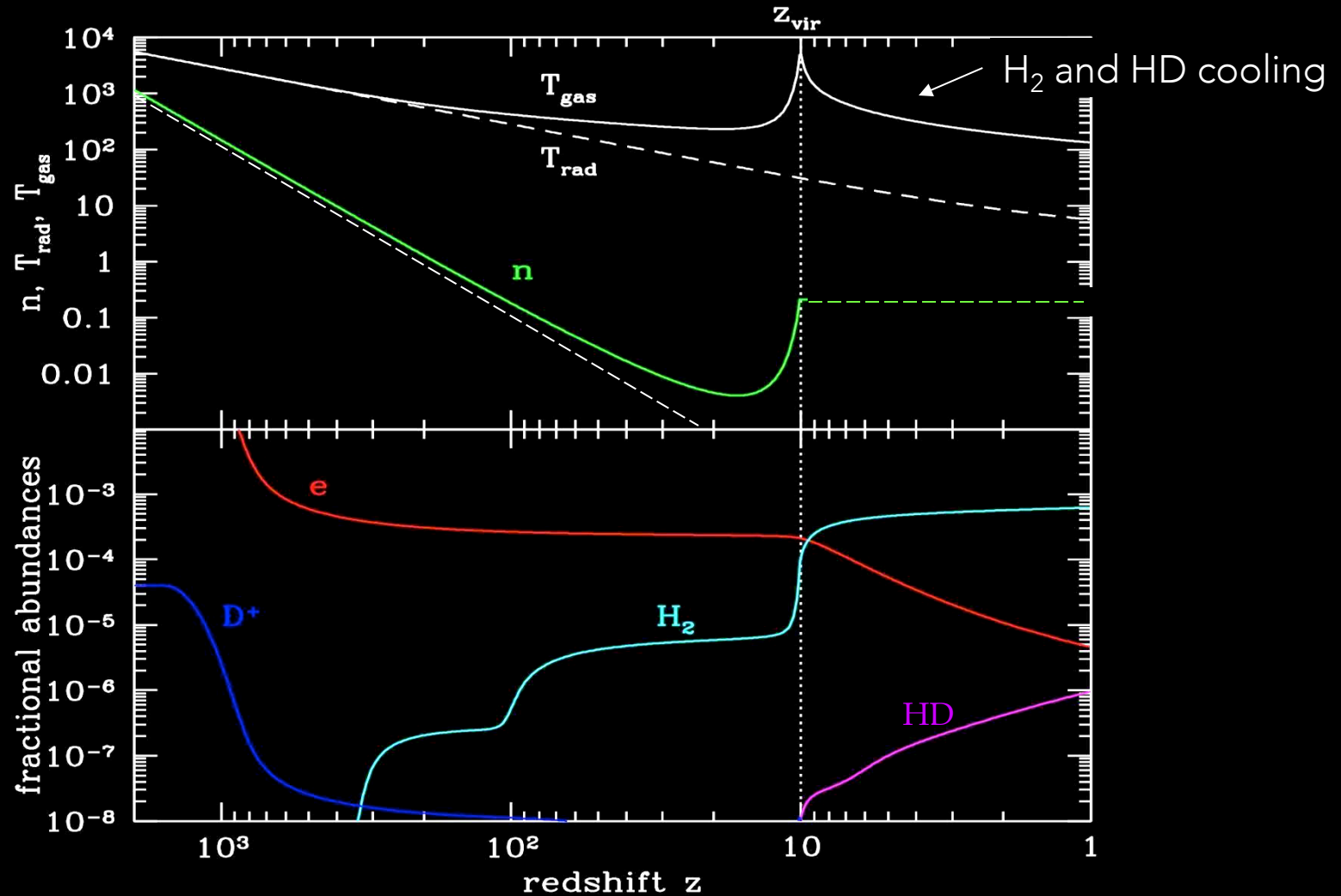


KROME!



Evolution of an overdense region

Tegmark et al. (1997), Galli & Palla (2002)



→ see talk by D. Schleicher on Tuesday

Radiative cooling of interstellar gas

- Present-day ISM:

Very efficient cooling. Abundant species with low-lying energy levels (rotational transitions of ^{12}CO , ^{13}CO , C^{18}O , fine-structure splitting of C^+ and O). Gas cooling also by collisions with dust grains.

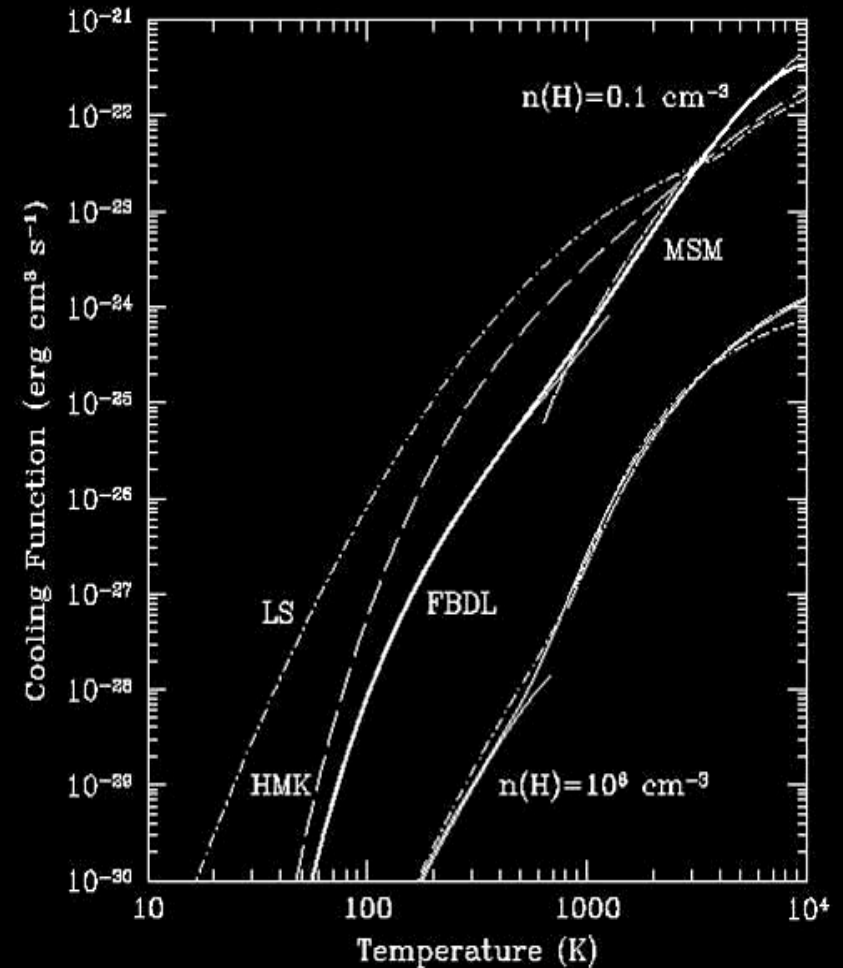
- Primordial Universe:

Inefficient cooling. Only H_2 and HD (minor species H_3^+ , LiH). Lowest transitions H_2 ($J=0-2$ with $\Delta T=510$ K, $J=1-3$ with $\Delta T=845$ K) and HD ($J=1-0$ with $\Delta T=128$ K, $J=2-1$ with $\Delta T=255$ K). Excitation of H_2 and HD by collisions with H followed by radiative decay.

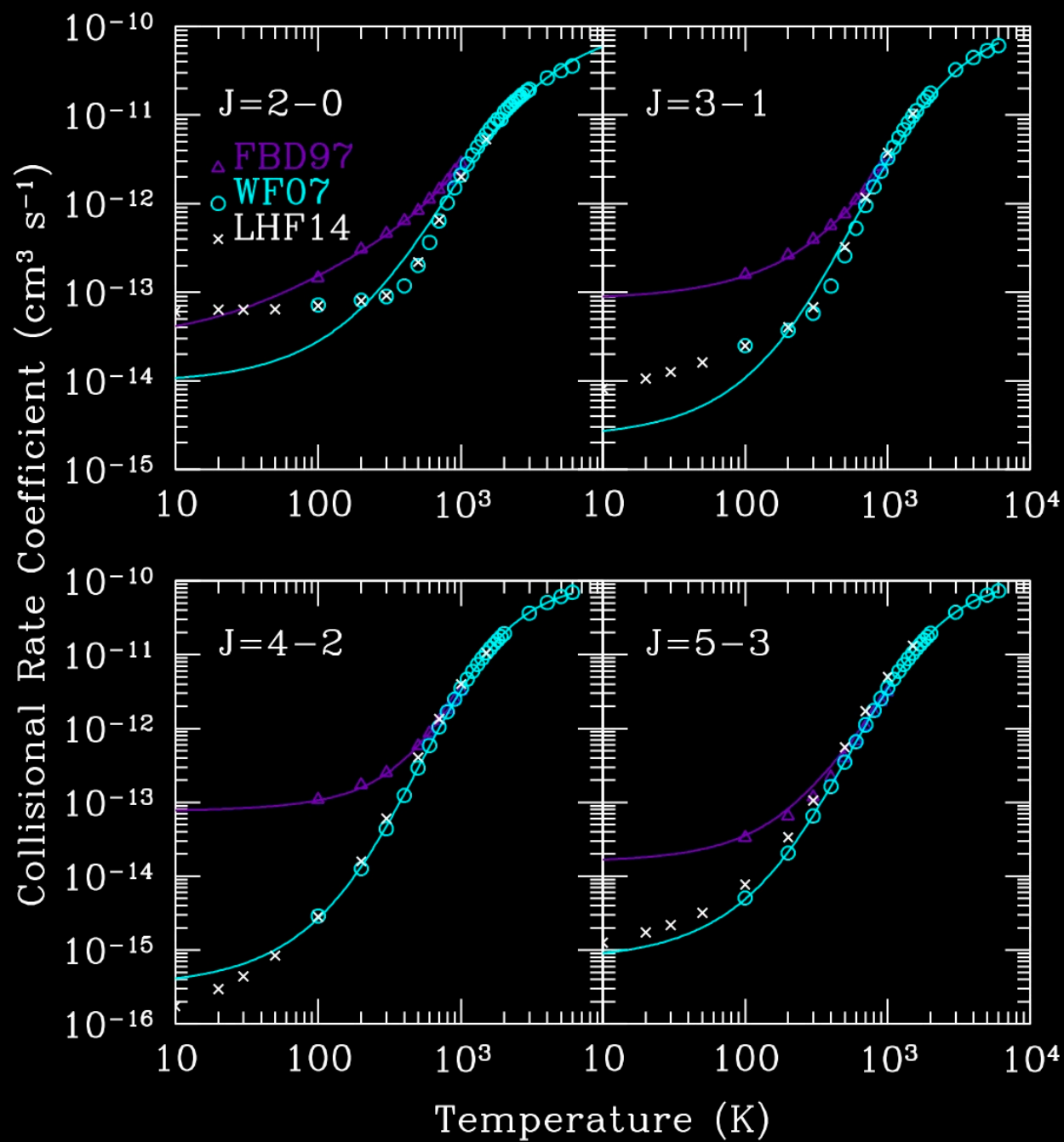
→ see talk by T. Grassi and S. Bovino on Tuesday

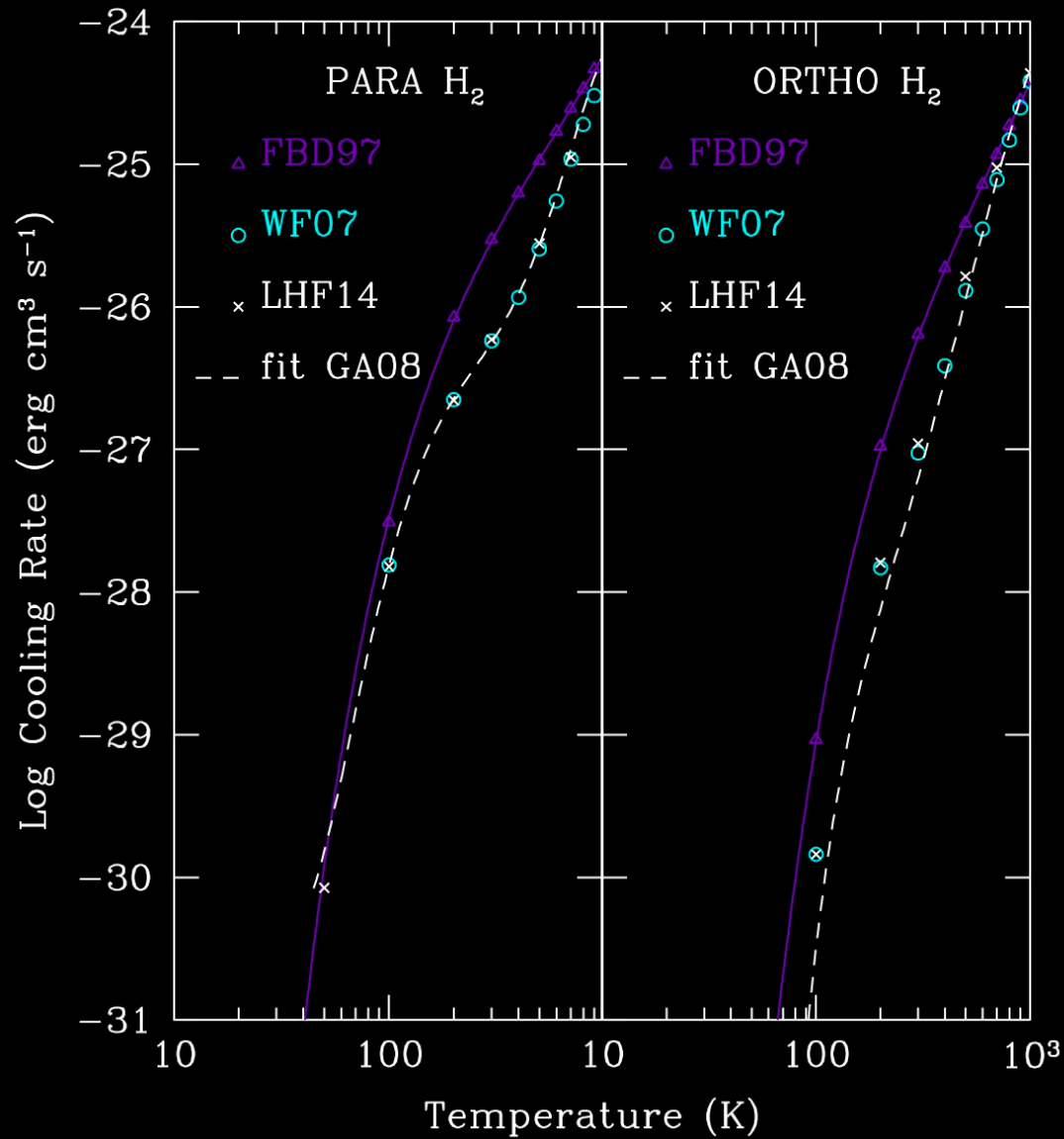
H₂ cooling

- Low-T rates for H-H₂ coll. exc. highly sensitive to adopted H₃ potential surface
- Galli & Palla (1998): coll. coeff. from Forrey et al. (1997) for $T < 600$ K, Mandy & Martin (1993) $T > 600$ K
- New set of H-H₂ coll. coeff. (Wrathmall & Flower 2007; Lique et al. 2014)
- H₂-H₂ (Flower 2000)
- He-H₂ (Flower et al. 1998; Balakrishnan et al. 1999)



Galli & Palla (1998)





Forrey et al. (1997), Wrathmall & Flower (2007), Lique et al. (2014)

Summary of primordial chemistry

- The first molecules are formed from gas-phase reactions after H and He recombination ($z < 1000$).
- H_2 , HD , and possibly H_3^+ control the thermodynamics of metal-free gas and determine the mass of the first stars. Li^+ controls the ionization fraction at high cloud densities.
- H^- , HeH^+ and Li dominate the optical depth of the primordial gas, but the induced spectral/spatial signatures in the CMB ($\Delta T/T < 10^{-7}$) are still below the sensitivity of current instruments ($\Delta T/T = 10^{-6}$).
- See Galli & Palla (2013) "The Dawn of Chemistry", ARAA vol. 51